#### CS444

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# Supervised Learning

- Stationoarity Assumption...
- Data is i.d.d.
  - Independent and identically distributed.
- Goal is to minimize loss on unobserved data from the same distribution.

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# Why Do Errors Happen?

#### (Informally) Three reasons:

- Bias Strong assumptions / excessive generalization
  - Representation Bias
  - 2 Search Bias
- 2 Variance Fitting insufficient training data so that performance is low on testing data.
- 3 Unavoidable/Irreducible error
- Bias and Variance are two sides of a coin: decreasing one tends to increase the other

"Bias/Variance Dilemma"

# **Evaluating Learning**

Training Set / Test Set

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Validation Set

### Using A Validation Set



Artificial Intelligence: Foundations of Computational Agents, Poole and Mackworth, 2010

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# Not Enough Data?

- K-fold cross-validation
- Leave-one-out cross-validation

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### Model Selection vs. Optimization

- Model selection Defines the hypothesis space.
- Optimization Finding the best hypothesis in that space.

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## Regularization

- Sort of like addressing the model selection problem through optimization.
- Change your loss metric to penalize complexity...

$$E(\boldsymbol{w}) = \sum_{j} (y_j - \boldsymbol{w}^T \boldsymbol{x}_j)^2 + \frac{\lambda}{2} \|\boldsymbol{w}\|^2$$

Solution:

$$\boldsymbol{w}^* = (\boldsymbol{X}^T \boldsymbol{X} + \lambda \boldsymbol{I})^{-1} \boldsymbol{X}^T \boldsymbol{y}$$

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