Discrete State Search for Robotics

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Generic Graph Search Algorithm (without weighted edges)

From our book:

```
Procedure GraphSearch(start, goal)
    OPEN := {start}
    CLOSED := {}
    found := False
   while (OPEN not empty) and (not found)
        Select a node n from OPEN.
        OPEN := OPEN - \{n\}
        CLOSED := CLOSED U {n}
        if n \in goal then
            found := True
        else
            Let M be the set of all states
            directly accessible from n which
            are not in CLOSED.
            OPEN := OPEN U M
```

Determines the order that states are searched.

Depth First Search

```
Procedure DFS(start, goal)
    OPEN := An empty stack.
    OPEN.push(start)
    CLOSED := {}
    found := False
    while (OPEN not empty) and (not found)
        n = OPEN.pop()
        CLOSED := CLOSED U {n}
        if n \in goal then
            found := True
        else
            for each state m accessible from n
                 if m \notin CLOSED and m \notin OPEN
                    OPEN.push(m)
```

Determines the order that states are searched.

Depth First Search

```
Procedure DFS(start, goal)

OPEN := An empty stack.

OPEN.push(start)

CLOSED := {}

found := False

while (OPEN not empty) and (not found)

n = OPEN.pop()

CLOSED := CLOSED U {n}

if n ∈ goal then

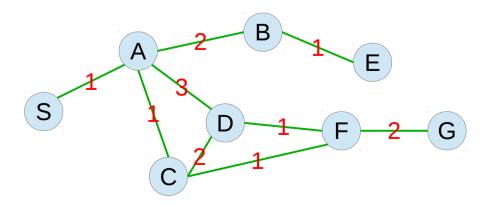
found := True

else

for each state m accessible from n

if m ∉ CLOSED and m ∉ OPEN

OPEN.push(m)
```



"Correct" version of Figure 6.1

Chosen	<u>Open</u>	<u>Closed</u>
_	S	_
S	Α	S
Α	B, C, D	A, S
D	B, C, F	A, S, D
F	B, C, G	A, S, D, F
G	В, С	A, S, D, G, F

Breadth First Search

```
Procedure BFS(start, goal)
    OPEN := An empty Queue.
    OPEN.enqueue(start)
    CLOSED := {}
    found := False
    while (OPEN not empty) and (not found)
        n = OPEN.dequeue()
        CLOSED := CLOSED U {n}
        if n \in goal then
            found := True
        else
            for each state m accessible from n
                if m ∉ CLOSED and m ∉ OPEN
                   OPEN.enqueue(m)
```

Determines the order that states are searched.

Search Nodes

```
Type SearchNode
State state
Node parent_node
Number path_cost

Function CreateSearchNode(State state, Node parent,
number step_cost)
Return a search node with
state = state
parent_node = parent
path_cost = step_cost + parent.path_cost
```

Generic Graph Search With Search Nodes

```
Function GraphSearch(start, goal)
    OPEN := { CreateSearchNode(start, NONE, 0) }
    CLOSED := {}
    found := False
    while (OPEN not empty) and (not found)
        Select a search node n from OPEN.
        OPEN := OPEN - \{n\}
        CLOSED := CLOSED U {n.state}
        if n.state \in goal then
            found := True
        else
            Let M be the set of all nodes
            directly accessible from n.state
            which are not in CLOSED.
            OPEN := OPEN U
                 \{SearchNode(m, n, cost n->m) \mid m \in M\}
    if found
        return a plan created by following
        parent links back from n
    else
        return FAILURE
```

Determines the order that states are searched.

Dijkstra's Algorithm

```
Procedure Dijkstra(start, goal)
    OPEN := An empty Priority Queue.
    n = SearchNode(start, NONE, 0)
    OPEN.enqueue(n, 0)
    CLOSED := {}
    found := False
   while (OPEN not empty) and (not found)
        n = OPEN.dequeue()
        CLOSED := CLOSED U {n.state}
        if n.state \in goal then
            found := True
        else
            for each node m accessible from n.state
                if m ∉ CLOSED and m ∉ any SearchNode in OPEN
                     m_node = SearchNode(m, n, cost of n->m)
                     OPEN.enqueue(m_node, m_node.path_cost)
    if found
        return a plan created by following
        parent links back from n
    else
        return FAILURE
```

(Missing detail: If m is already in a node in OPEN, then that node should be replaced if m_node has a lower cost.)

Dijkstra's Algorithm

```
Procedure Dijkstra(start, goal)
   OPEN := An empty Priority Queue.
   n = SearchNode(start, NONE, 0)
   OPEN.enqueue(n, 0)
   CLOSED := {}
   found := False
   while (OPEN not empty) and (not found)
       n = OPEN.dequeue()
       CLOSED := CLOSED U {n.state}
        if n.state \in goal then
            found := True
        else
            for each node m accessible from n.state
                if m ∉ CLOSED and m ∉ any SearchNode in OPEN
                     m_node = SearchNode(m, n, cost of n->m)
                     OPEN.enqueue(m_node, m_node.path_cost)
    if found
        return a plan created by following
        parent links back from n
    else
        return FAILURE
```

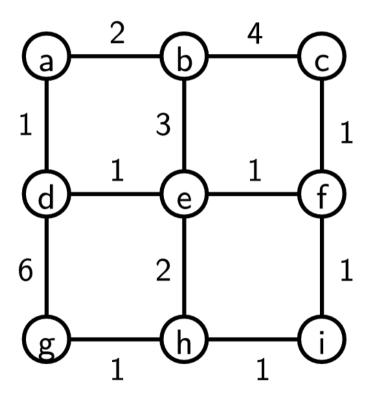
A*

• Exactly like Djikstra's, Except, priority is calculated as:

$$\begin{split} f(n) &= g(n) + h(n) \\ g(n) &= \text{Total path cost to that node} \\ h(n) &= \text{Estimated cost to the goal} \end{split}$$

 As long as h(n) doesn't overestimate, A* is guaranteed to find an optimal path.

Exercise



A* Heuristic

h(n) = Minimum number of edgesbetween n and the goal.

For example (assuming the goal is a)

$$h(g) = 2$$

$$h(i) = 4$$

Since all weights are at least 1, this is guaranteed not to overestimate the path cost.

Exercise

• Fill out Chosen/Open/Closed tables (like figures 6.1-6.3) and the final path for:

```
- DFS: start=g, goal=a
```

- All "ties" should be broken by alphabetical order: State 'a' is selected before state 'b'
- For DFS and BFS, the Open column should be formatted as follows:

• For Dijkstra, the Open column should be formatted as follows:

```
(state, parent, path_cost)
```

• For A*, the Open column should be formatted as follows:

```
(state, parent, path_cost, f(n))
```