

Discrete State Search for Robotics

CS354
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Generic Graph Search Algorithm (without weighted edges)

From our book:

```
Procedure GraphSearch(start, goal)
  OPEN := {start}
  CLOSED := {}
  found := False
  while (OPEN not empty) and (not found)
    Select a node n from OPEN.
    OPEN := OPEN - {n}
    CLOSED := CLOSED U {n}
    if n ∈ goal then
      found := True
    else
      Let M be the set of all nodes
      directly accessible from n which
      are not in CLOSED.
      OPEN := OPEN U M
```

Determines
the order that
states are
searched.

Depends on the
problem

Depth First Search

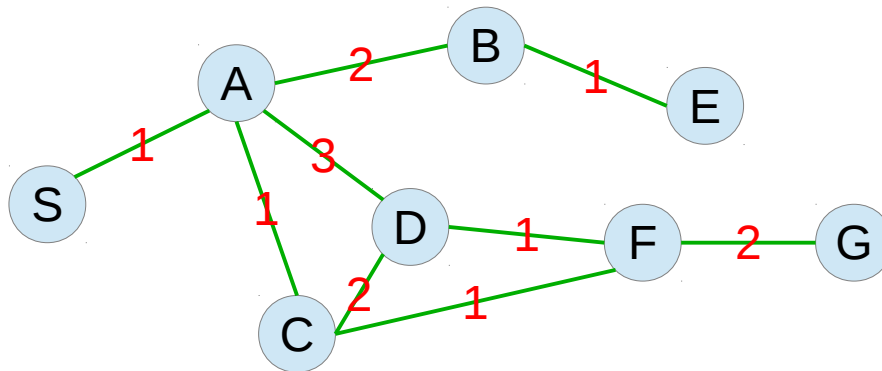
```
Procedure DFS(start, goal)
  OPEN := An empty stack.
  OPEN.push(start)
  CLOSED := {}
  found := False
  while (OPEN not empty) and (not found)
    n = OPEN.pop()
    CLOSED := CLOSED U {n}
    if n ∈ goal then
      found := True
    else
      for each state m accessible from n
        if m ∉ CLOSED and m ∉ OPEN
          OPEN.push(m)
```

Determines
the order that
states are
searched.

Depends on the
problem

Depth First Search

```
Procedure DFS(start, goal)
  OPEN := An empty stack.
  OPEN.push(start)
  CLOSED := {}
  found := False
  while (OPEN not empty) and (not found)
    n = OPEN.pop()
    CLOSED := CLOSED U {n}
    if n ∈ goal then
      found := True
    else
      for each state m accessible from n
        if m ∉ CLOSED and m ∉ OPEN
          OPEN.push(m)
```



“Correct” version of Figure 6.1

<u>Chosen</u>	<u>Open</u>	<u>Closed</u>
-	S	-
S	A	S
A	B, C, D	A, S
D	B, C, F	A, S, D
F	B, C, G	A, S, D, F
G	B, C	A, S, D, G, F

Breadth First Search

```
Procedure BFS(start, goal)
  OPEN := An empty Queue.
  OPEN.enqueue(start)
  CLOSED := {}
  found := False
  while (OPEN not empty) and (not found)
    n = OPEN.dequeue()
    CLOSED := CLOSED U {n}
    if n ∈ goal then
      found := True
    else
      for each state m accessible from n
        if m ∉ CLOSED and m ∉ OPEN
          OPEN.enqueue(m)
```

Determines
the order that
states are
searched.

Depends on the
problem

Search Nodes

Type Node

```
State  state
Node   parent_node
Number path_cost
```

```
Function CreateNode(State state, Node parent,
                    number step_cost)
```

Return a node with

```
state = state
parent_node = parent
path_cost = step_cost + parent.path_cost
```

Generic Graph Search With Nodes

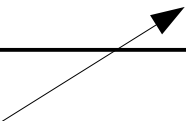
```
Function GraphSearch(start, goal)
  OPEN := { CreateNode(start, NONE, 0) }
  CLOSED := {}
  found := False
  while (OPEN not empty) and (not found)
    Select a node n from OPEN.
    OPEN := OPEN - {n}
    CLOSED := CLOSED U {n.state}
    if n.state ∈ goal then
      found := True
    else
      Let M be the set of all nodes
      directly accessible from n which
      are not in CLOSED.
      OPEN := OPEN U M
  if found
    return a plan created by following
    parent links back from n
  else
    return FAILURE
```

Determines
the order that
states are
searched.

Depends on the
problem

Dijkstra's Algorithm

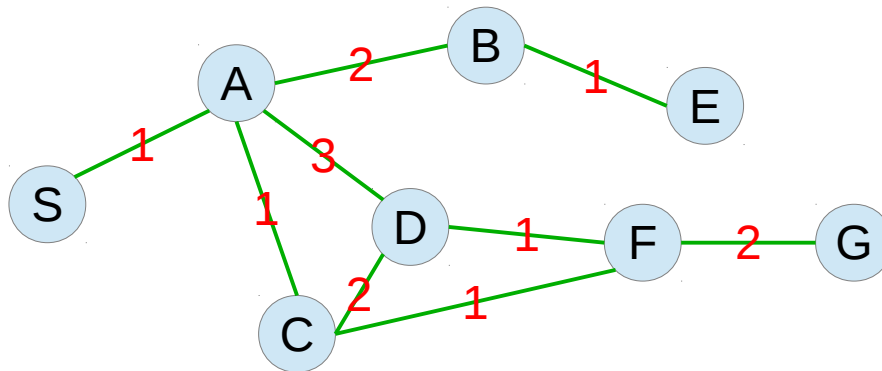
```
Procedure Dijkstra(start, goal)
  OPEN := An empty Priority Queue.
  n = CreateNode(start, NONE, 0)
  OPEN.enqueue(n, 0)
  CLOSED := {}
  found := False
  while (OPEN not empty) and (not found)
    n = OPEN.dequeue()
    CLOSED := CLOSED U {n.state}
    if n.state ∈ goal then
      found := True
    else
      for each state m accessible from n
        if m ∉ CLOSED and m ∉ Any Node in OPEN
          m_node = CreateNode(m, n, Cost of n->m)
          OPEN.enqueue(m_node, m_node.path_cost)
```



(Missing detail: If m is already in a node in OPEN, then that node should be replaced if m_node has a lower cost.)

Dijkstra's Algorithm

```
Procedure Dijkstra(start, goal)
  OPEN := An empty Priority Queue.
  n = CreateNode(start, NONE, 0)
  OPEN.enqueue(n, 0)
  CLOSED := {}
  found := False
  while (OPEN not empty) and (not found)
    n = OPEN.dequeue()
    CLOSED := CLOSED U {n.state}
    if n.state ∈ goal then
      found := True
    else
      for each state m accessible from n
        if m ∉ CLOSED and m ∉ Any Node in OPEN
          m_node = CreateNode(m, n, Cost of n->m)
          OPEN.enqueue(m_node, m_node.path_cost)
```



A*

- Exactly like Dijkstra's, Except, priority is calculated as:

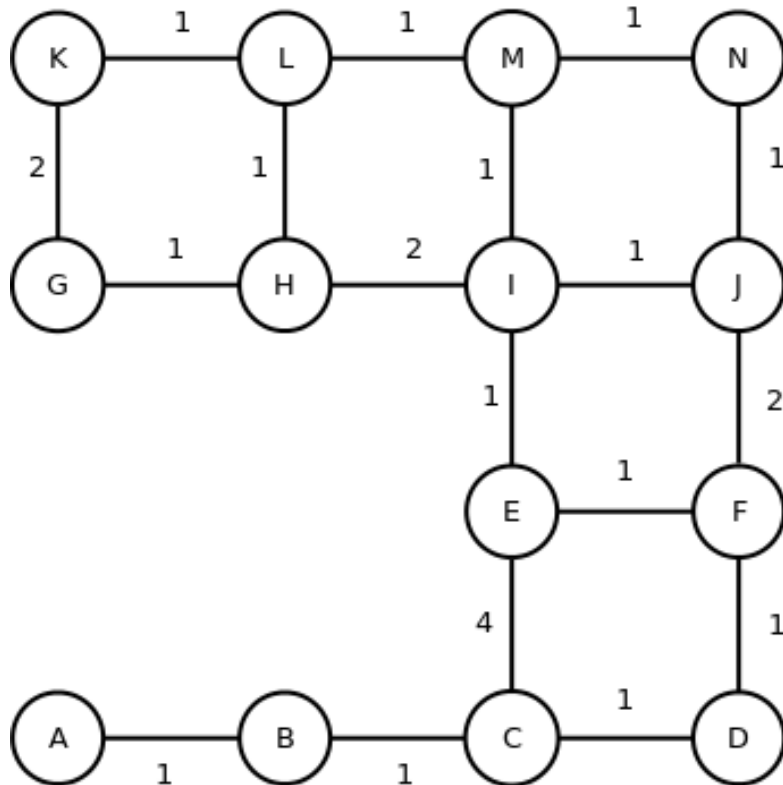
$$f(n) = g(n) + h(n)$$

$g(n)$ = Total path cost to that node

$h(n)$ = Estimated cost to the goal

- As long as $h(n)$ doesn't overestimate, A* is guaranteed to find an optimal path.

Exercise



A* Heuristic

$h(n)$ = Minimum number of edges between n and the goal.

For example:

$$h(C) = 2$$

$$h(G) = 6$$

Since all weights are at least 1, this is guaranteed not to overestimate the path cost.

Exercise

- Fill out Chosen/Open/Closed tables (like figures 6.1-6.3) and the final path for:
 - DFS: start=I, goal=A
 - BFS: start=I, goal=A
 - Dijkstra: start=E, goal=A
 - A*: start=E, goal=A
- All “ties” should be broken by alphabetical order: State 'A' is selected before state 'B'
- For DFS and BFS, the Open column should be formatted as follows:
(state, parent), e.g. ('A', 'B')
- For Dijkstra, the Open column should be formatted as follows:
(state, parent, path_cost)
- For A*, the Open column should be formatted as follows:
(state, parent, path_cost, f(n))