## CS354

#### Nathan Sprague

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- Two issues to consider today:
  - How to efficiently and conveniently encode a map of the robot's environment?

- How to parameterize the configuration of the robot?
- Both questions need to be addressed in order to plan.

#### Grid Based Maps

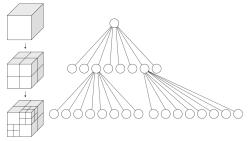
- Recall:
  - Easy to work with, not space efficient
  - $\blacksquare$  Naive 2d grid representation of a 10m  $\times$  10m room at 1cm accuracy:

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### Grid Based Maps

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    - $1000 \times 1000 = 1,000,000$  cells
- Quadtree is a more space efficient alternative...
- Octree is the 3d generalization



http://en.wikipedia.org/wiki/File:Octree2.svg, http://creativecommons.org/licenses/by-sa/3.0/

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# **Topological Maps**

• "A configuration  $\mathbf{q} \in C$  of the robot  $\mathcal{A}$  is a specification of the state of  $\mathcal{A}$  with respect to a fixed frame  $F_w$ " (Dudek and Jenkin)

**Turtlebot configuration:**  $\mathbf{q} = [x, y, \Theta]$ .

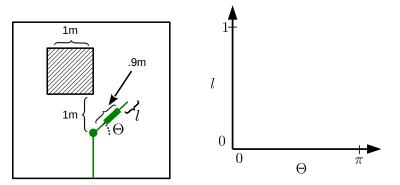
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- Turtlebot configuration:  $\mathbf{q} = [x, y, \Theta]$ .
- A **C-Obstacle** *CB<sub>i</sub>* is defined as:
  - $\blacksquare \ \mathcal{C}B_i = \{\mathbf{q} \in \mathcal{C} \mid \mathcal{A}(\mathbf{q}) \cap \mathcal{B}_i \neq \emptyset\}$ 
    - **\square**  $\mathcal{B}_i$  is the space occupied by obstacle *i*.
    - $\mathcal{A}(\mathbf{q})$  is the space occupied by the robot in configuration  $\mathbf{q}$ .

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• 
$$C_{free} = \{ \mathbf{q} \in C \mid \mathcal{A}(\mathbf{q}) \cap (\cup_i \mathcal{B}_i) = \emptyset \}$$
  
•  $C_{obs} = \overline{C_{free}}$ 

Exercise

Draw  $C_{free}$  for this robot:



Robot arm with a single rotational joint and a single prismatic joint

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- I prismatic joint extension in meters
- $\Theta$  angle of rotational joint ( $\Theta \approx \pi/4$  in the image)

 "A free path in C-space is a continuous curve exclusively in *C*<sub>free</sub> that connects two configurations **q**<sub>start</sub> and **q**<sub>goal</sub>."

- Paths may be
  - free: obstacles are not touched.
  - semi-free: obstacles may be touched.
- The goal of planning is to find a path.

- Holonomic vs. Non-holonomic constraints
  - Holonomic constraints restrict the allowed configurations.
  - Non-Holonomic constraints put limits on the paths between configurations.

- Point robot assumption and object dilation
  - Simplifies the problem of finding C<sub>free</sub>