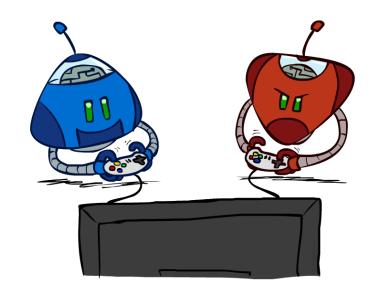


Artificial Intelligence





CS 444 – Spring 2021

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Department of Computer Science

James Madison University



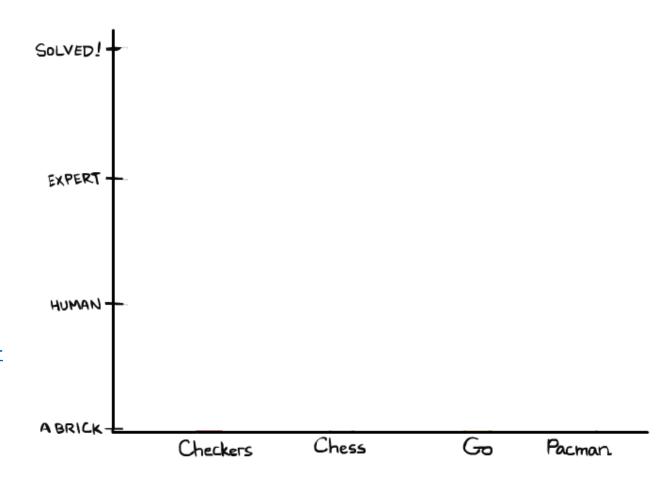




Today

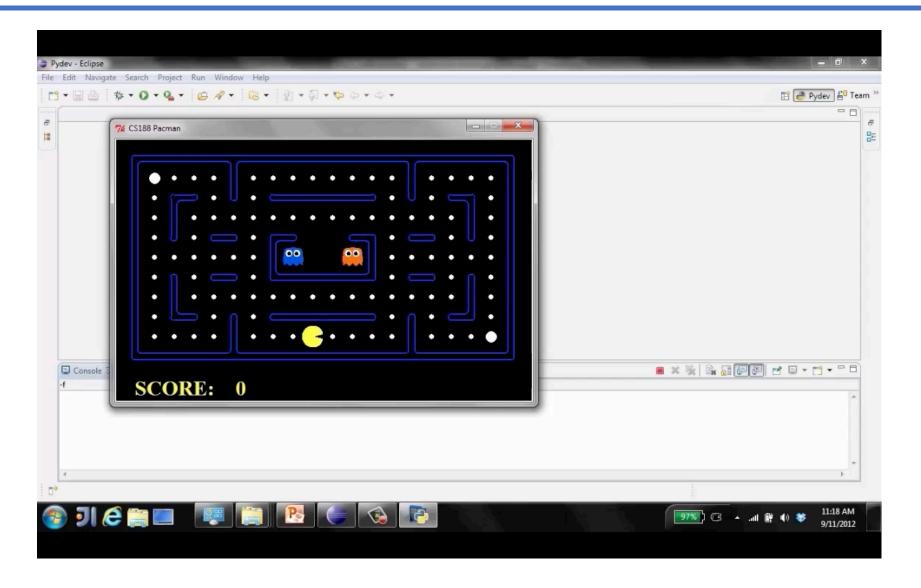
- Checkers: 1950: First computer player. 1994: First computer champion: Chinook ended 40-year-reign of human champion Marion Tinsley using complete 8-piece endgame. 2007: Checkers solved!
- Chess: 1997: Deep Blue defeats human champion Gary Kasparov in a six-game match. Deep Blue examined 200M positions per second, used very sophisticated evaluation and undisclosed methods for extending some lines of search up to 40 ply. Current programs are even better, if less historic.
- Go: Human champions are now starting to be challenged by machines. In go, b > 300! Classic programs use pattern knowledge bases, but big recent advances use neural networks developed by Google's DeepMind research group (Alpha Go -https://deepmind.com/research/case-studies/alphagothe-story-so-far)

Pacman





What is Going On Under the Covers?





Types of Games

Many different kinds of games!

- Axes:
 - Deterministic or stochastic?
 - One, two, or more players?
 - Zero sum?
 - Perfect information (can you see the state)?



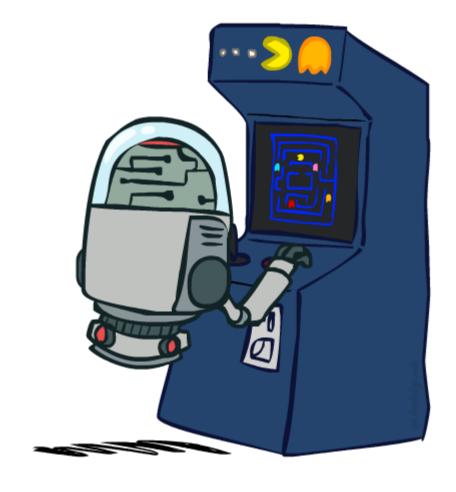
 Want algorithms for calculating a strategy (policy) which recommends a move from each state



Deterministic Games

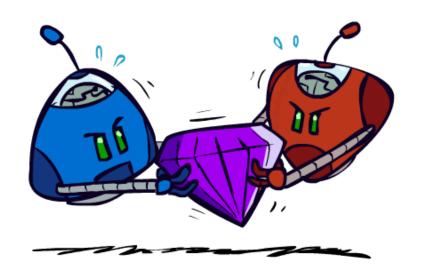
- Many possible formalizations, one is:
 - States: S (start at s₀)
 - Players: P={1...N} (usually take turns)
 - Actions: A (may depend on player / state)
 - Transition Function: $SxA \rightarrow S$
 - Terminal Test: $S \rightarrow \{t,f\}$
 - Terminal Utilities: $SxP \rightarrow R$

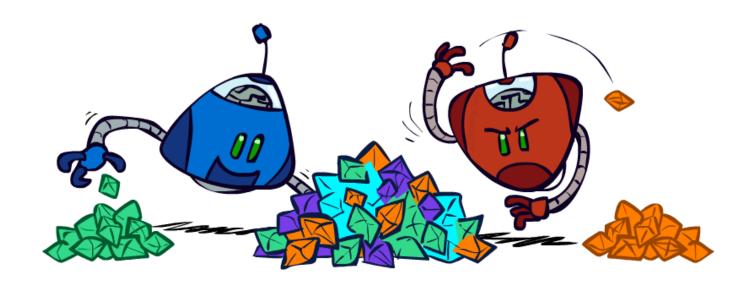
• Solution for a player is a policy: $S \rightarrow A$





Zero-Sum Games





Zero-Sum Games

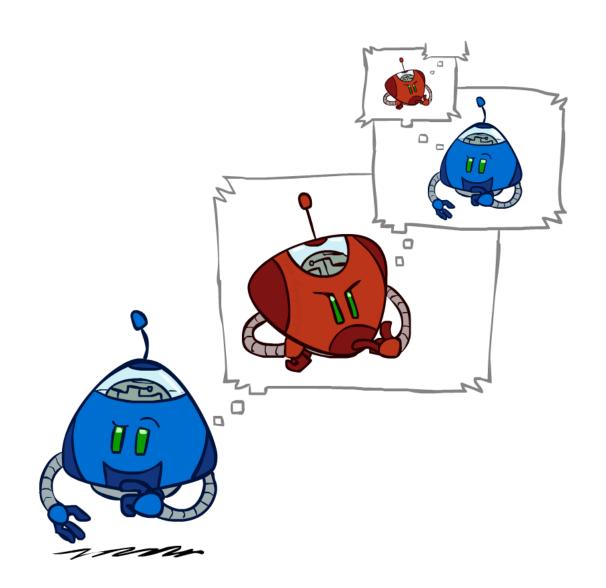
- Agents have opposite utilities (values on outcomes)
- Lets us think of a single value that one maximizes and the other minimizes
- Adversarial, pure competition

General Games

- Agents have independent utilities (values on outcomes)
- Cooperation, indifference, competition, and more are all possible
- More later on non-zero-sum games

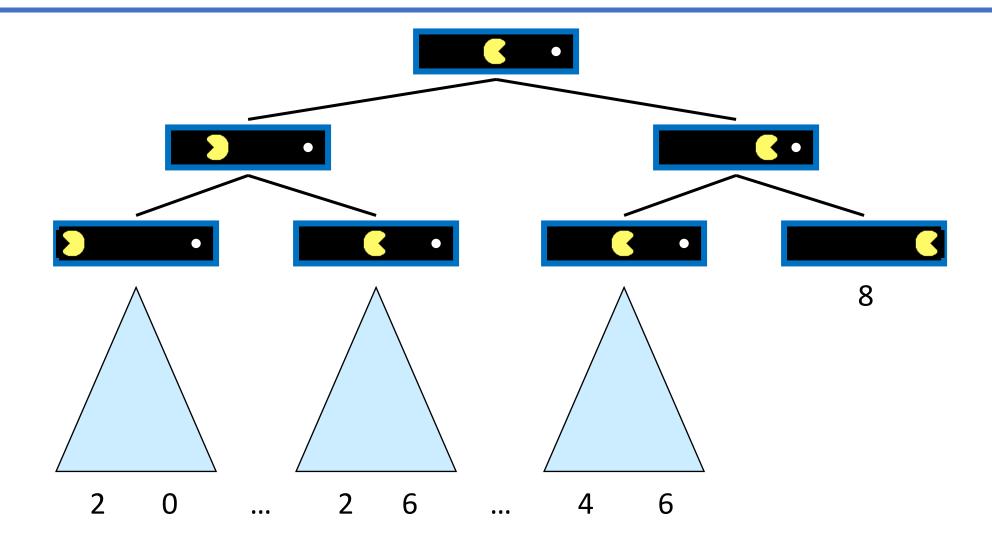


Adversarial Search





Single-Agent Trees



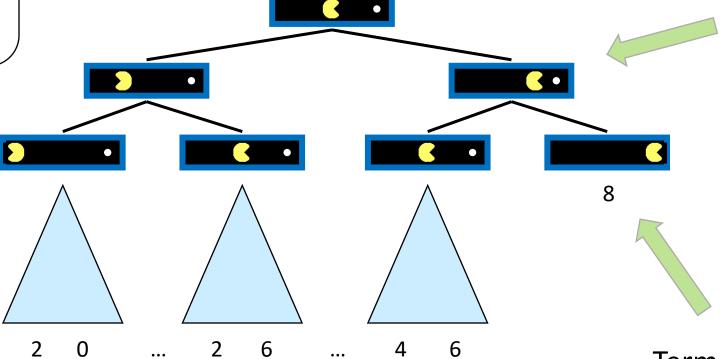


Value of a State

Value of a state:
The best achievable outcome (utility)
from that state

Non-Terminal States:

$$V(s) = \max_{s' \in \text{children}(s)} V(s')$$

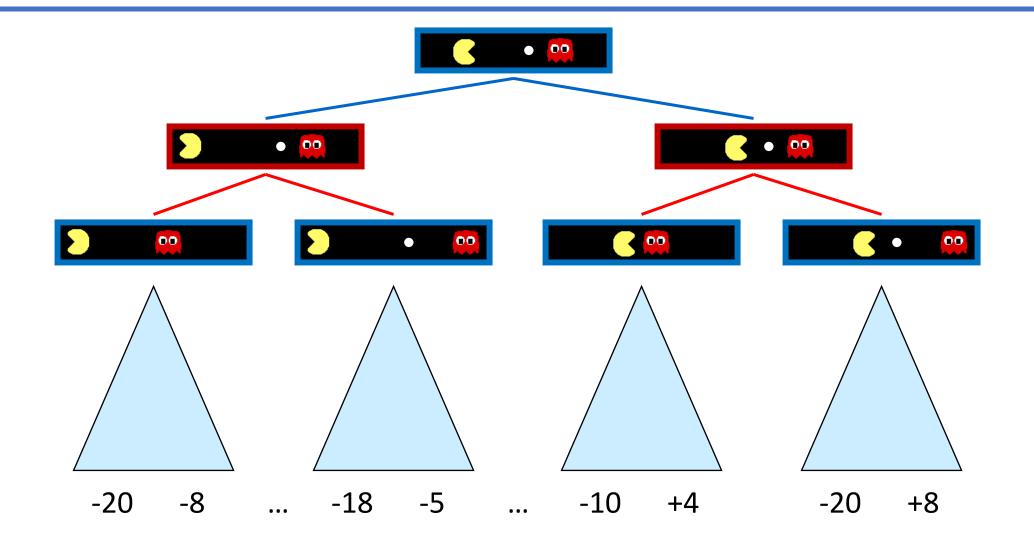


Terminal States:

$$V(s) = \text{known}$$



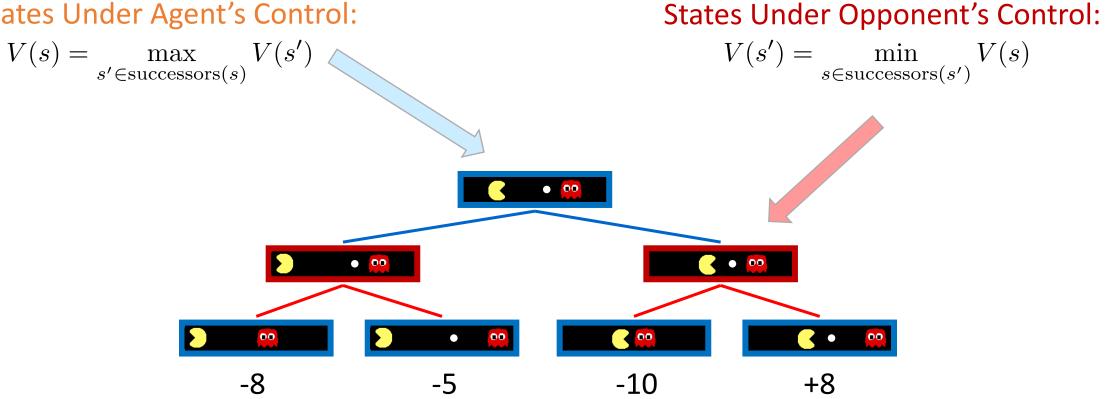
Adversarial Game Trees





Minimax Values

States Under Agent's Control:

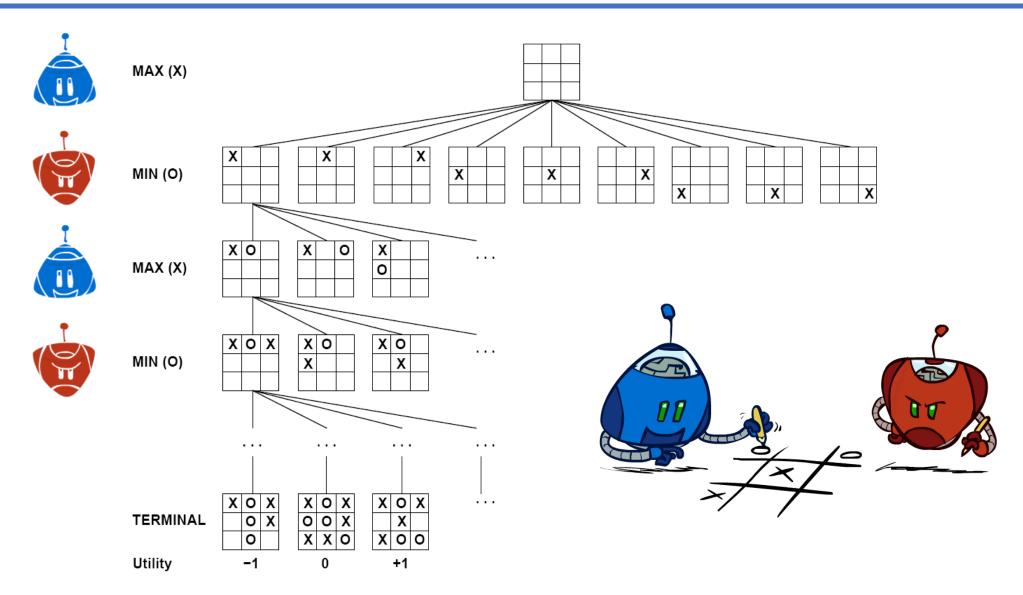


Terminal States:

$$V(s) = \text{known}$$



Tic-Tac-Toe Game Tree

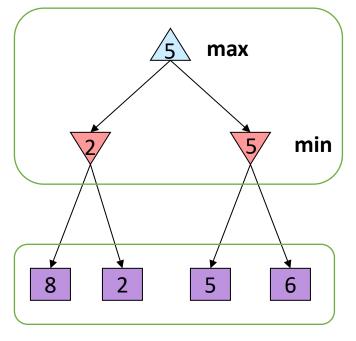




Adversarial Search (Minimax)

- Deterministic, zero-sum games:
 - Tic-tac-toe, chess, checkers
 - One player maximizes result
 - The other minimizes result
- Minimax search:
 - A state-space search tree
 - Players alternate turns
 - Compute each node's minimax value: the best achievable utility against a rational (optimal) adversary

Minimax values: computed recursively



Terminal values: part of the game



Minimax Implementation

def max-value(state):

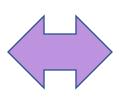
initialize $v = -\infty$

for each successor of state:

v = max(v, min-value(successor))

return v

$$V(s) = \max_{s' \in \text{successors}(s)} V(s')$$



def min-value(state):

initialize $v = +\infty$

for each successor of state:

v = min(v, max-value(successor))

return v

$$V(s') = \min_{s \in \text{successors}(s')} V(s)$$

Minimax Implementation (Dispatch)

```
def value(state):
    if the state is a terminal state: return the state's utility
    if the next agent is MAX: return max-value(state)
    if the next agent is MIN: return min-value(state)
```

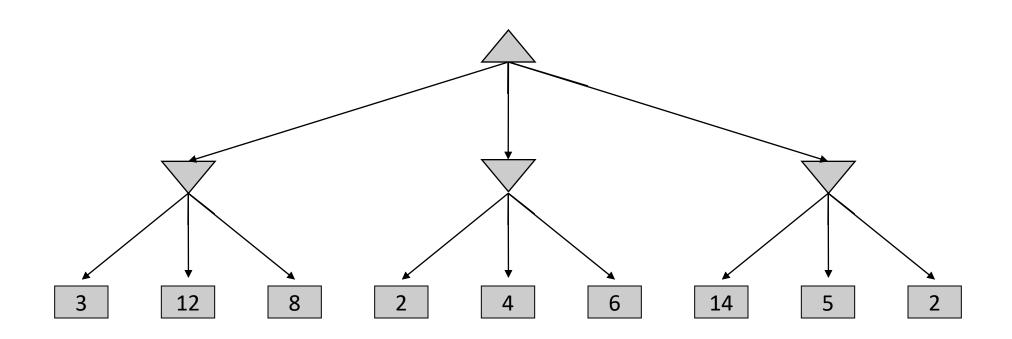
def max-value(state):

```
initialize v = -∞
for each successor of state:
    v = max(v, value(successor))
return v
```

```
def min-value(state):
    initialize v = +∞
    for each successor of state:
        v = min(v, value(successor))
    return v
```



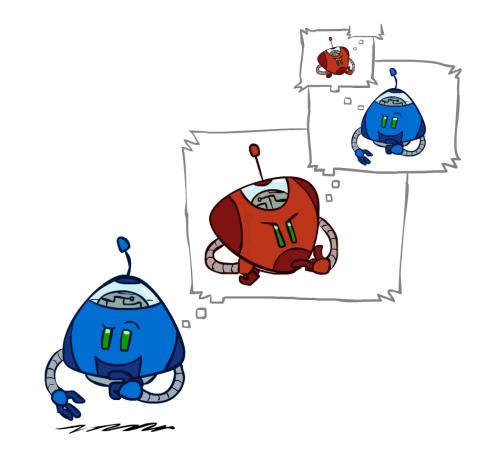
Minimax Example





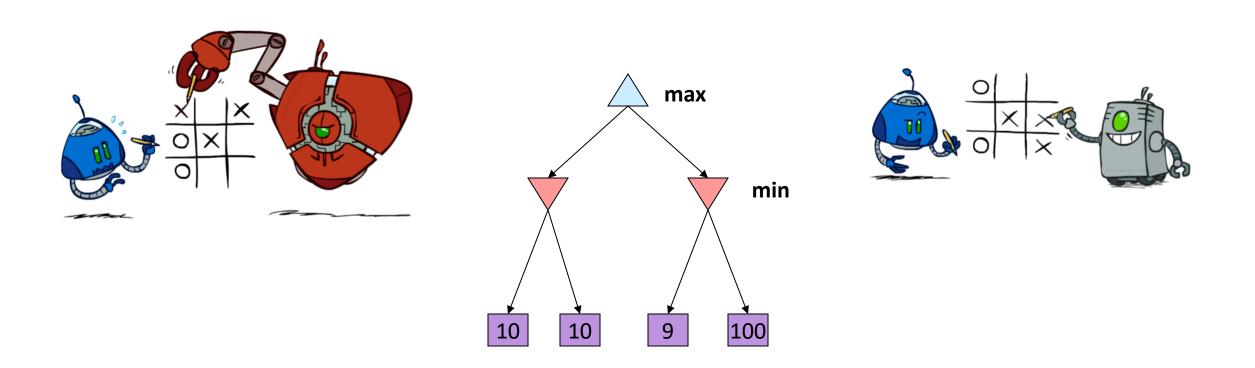
Minimax Efficiency

- How efficient is minimax?
 - Just like (exhaustive) DFS
 - Time: O(b^m)
 - Space: O(bm)
- Example: Chess, b ≈35, m ≈ 100
 - Exact solution is completely infeasible
 - Do we need to explore the entire tree?





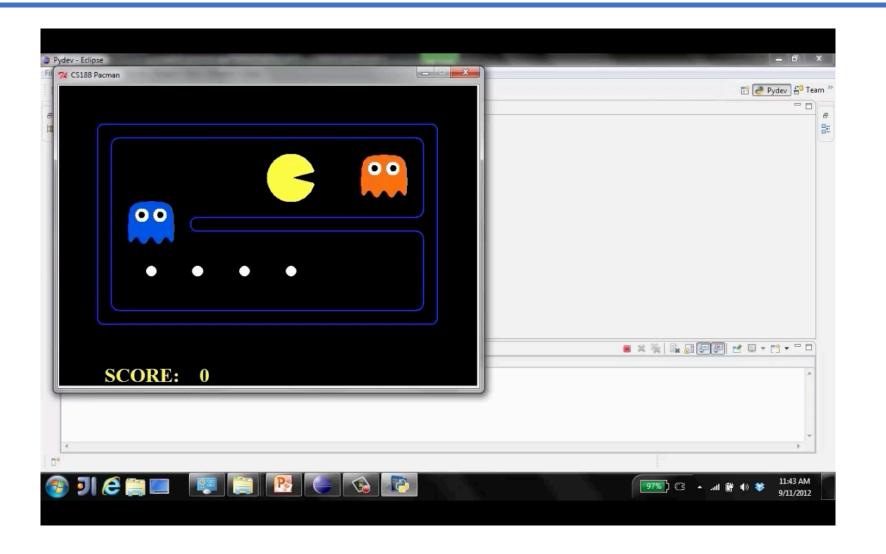
Minimax Properties



Optimal against a perfect player. Otherwise?

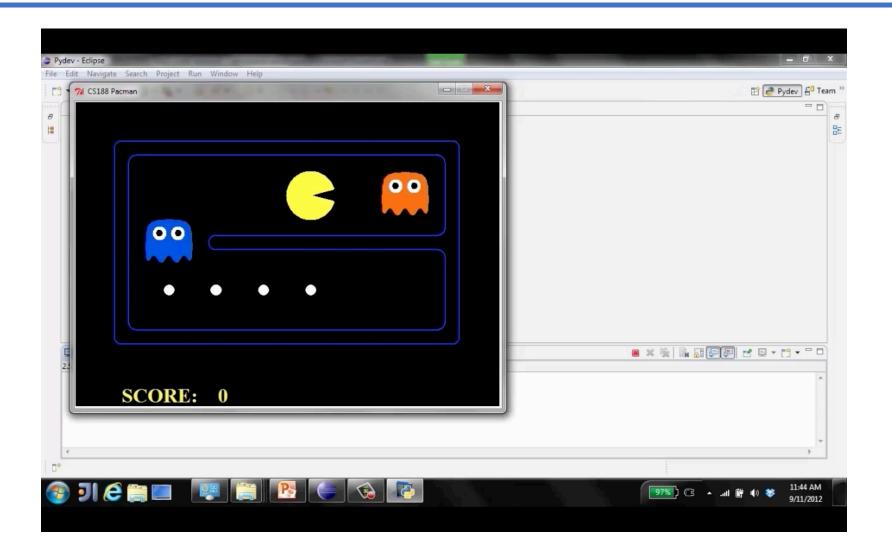


Video of Demo Min Vs Exp (Min)





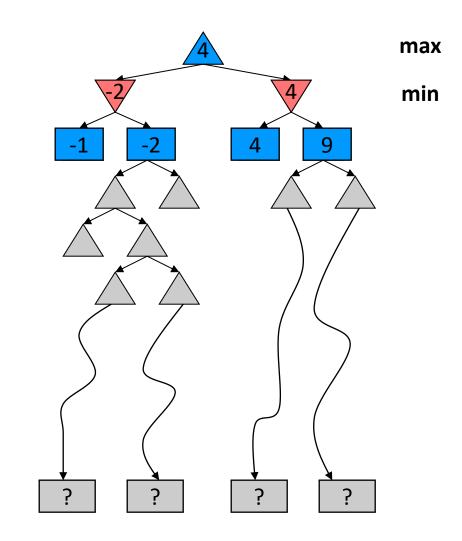
Video of Demo Min vs Exp (Exp)





Resource Limits

- Problem: In realistic games, cannot search to leaves!
- Solution: Depth-limited search
 - Instead, search only to a limited depth in the tree
 - Replace terminal utilities with an evaluation function for nonterminal positions
- Example:
 - Suppose we have 100 seconds, can explore 10K nodes / sec
 - So can check 1M nodes per move
 - α - β reaches about depth 8 decent chess program
- Guarantee of optimal play is gone
- More plies makes a BIG difference
- Use iterative deepening for an anytime algorithm

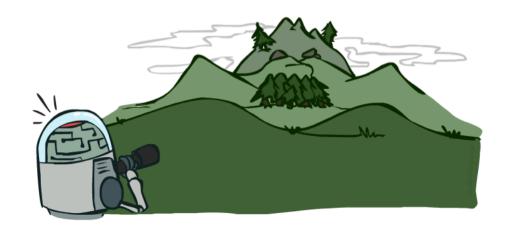




Search Depth Matters

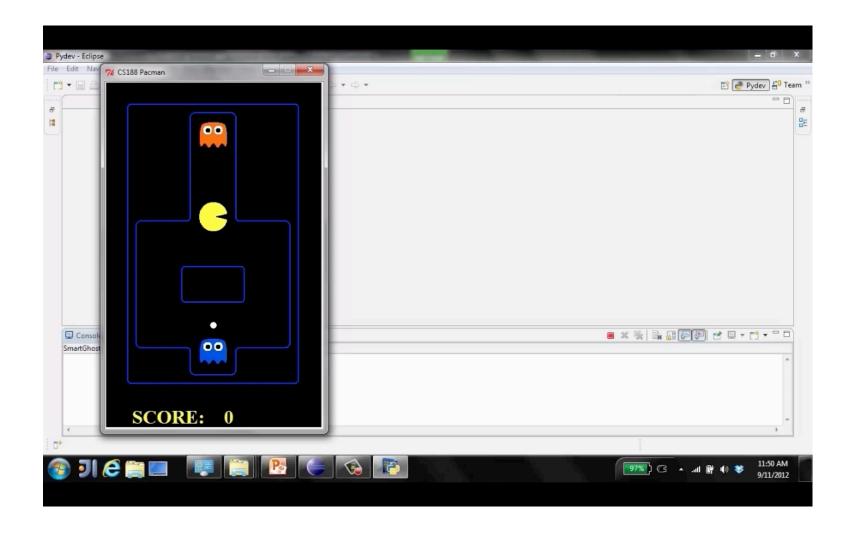
- Evaluation functions are always imperfect
- The deeper in the tree the evaluation function is buried, the less the quality of the evaluation function matters
- An important example of the tradeoff between complexity of features and complexity of computation





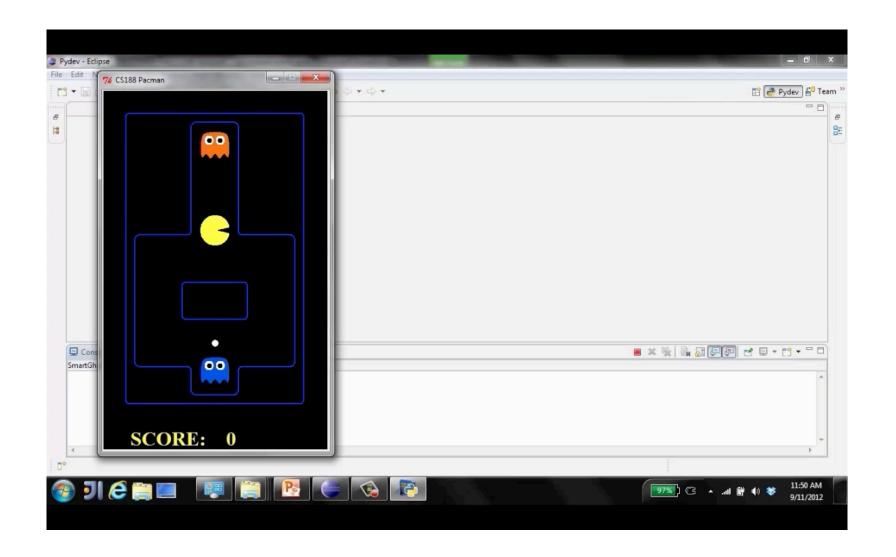


Demo Limited Depth (2)





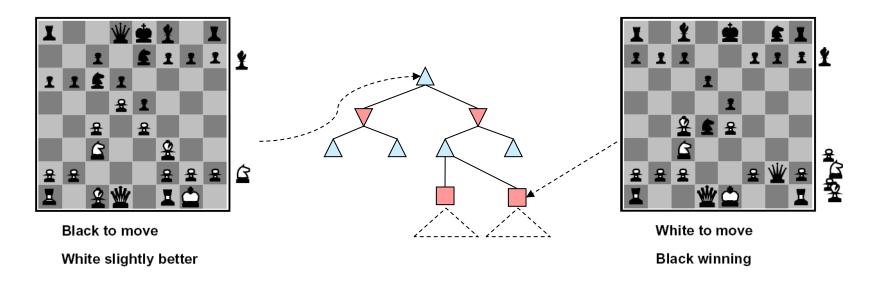
Demo – Depth Limited (10)





Evaluation Functions

Evaluation functions score non-terminals in depth-limited search



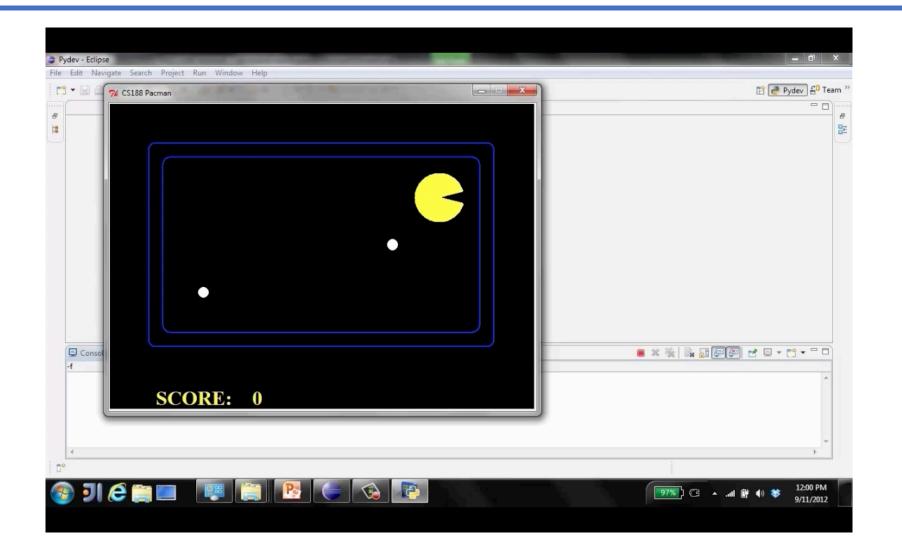
- Ideal function: returns the actual minimax value of the position
- In practice: typically weighted linear sum of features:

$$Eval(s) = w_1 f_1(s) + w_2 f_2(s) + \dots + w_n f_n(s)$$

• e.g. $f_1(s)$ = (num white queens – num black queens), etc.

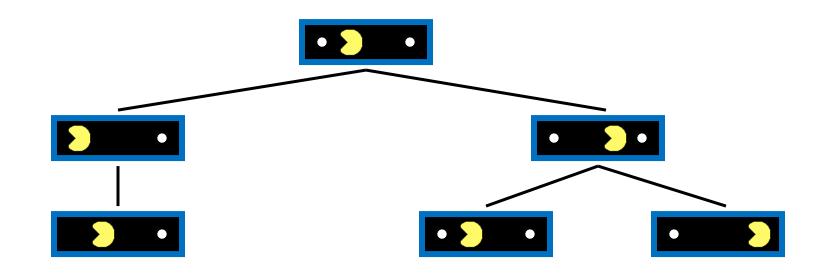


Evaluation for Pacman – Thrashing (d=2)





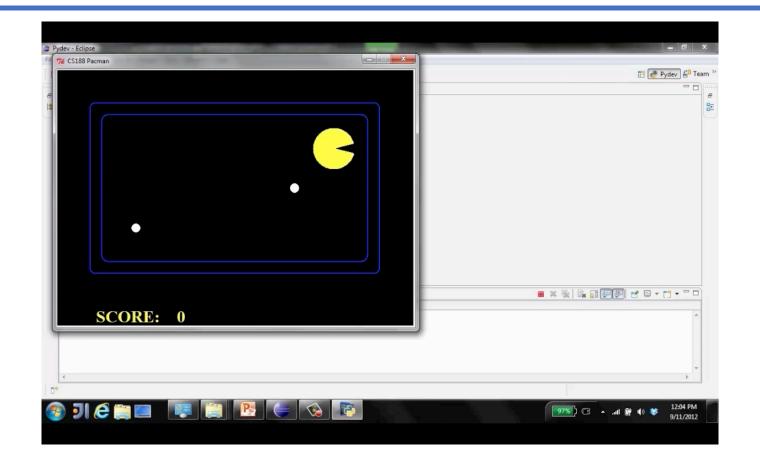
Why does Pacman Thrash and Starve



- A danger of replanning agents!
 - He knows his score will go up by eating the dot now (west, east)
 - He knows his score will go up just as much by eating the dot later (east, west)
 - There are no point-scoring opportunities after eating the dot (within the horizon, two here)
 - Therefore, waiting seems just as good as eating: he may go east, then back west in the next round of replanning!



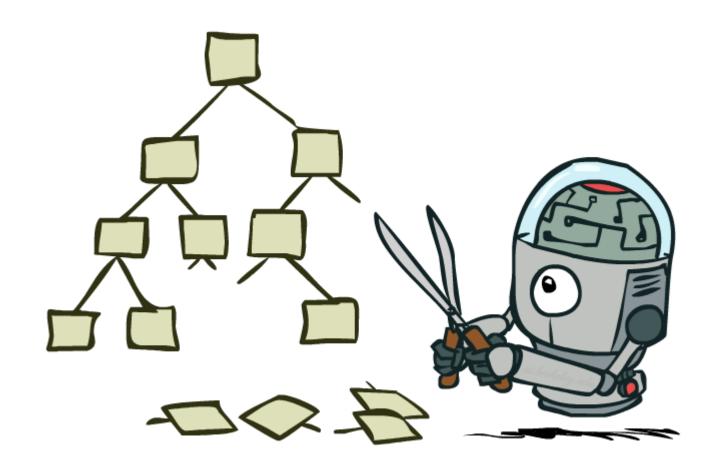
Video – Thrashing Resolved – Fixed (d=2)



Evaluation function includes proximity to the nearest food pellet.

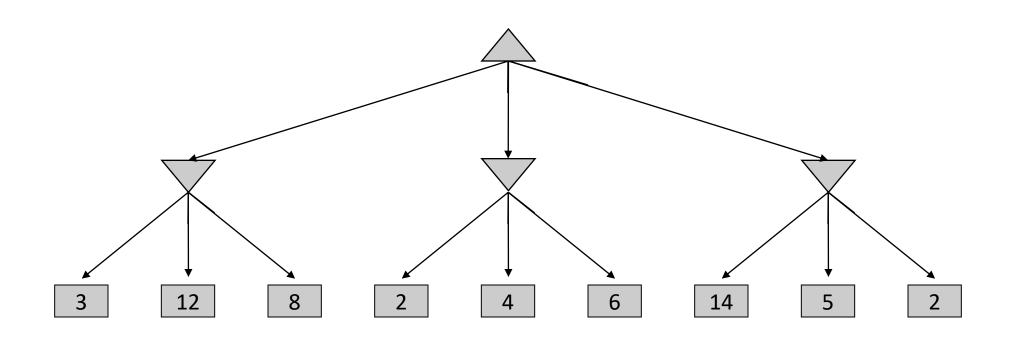


Game Tree Pruning





Game Tree Pruning

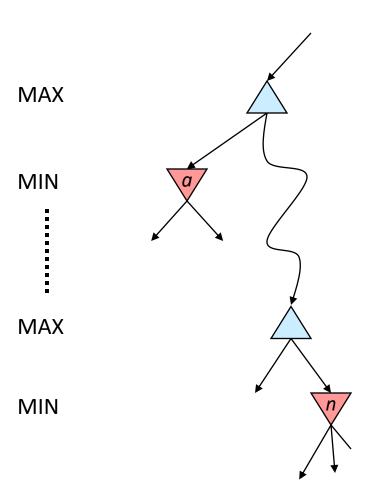




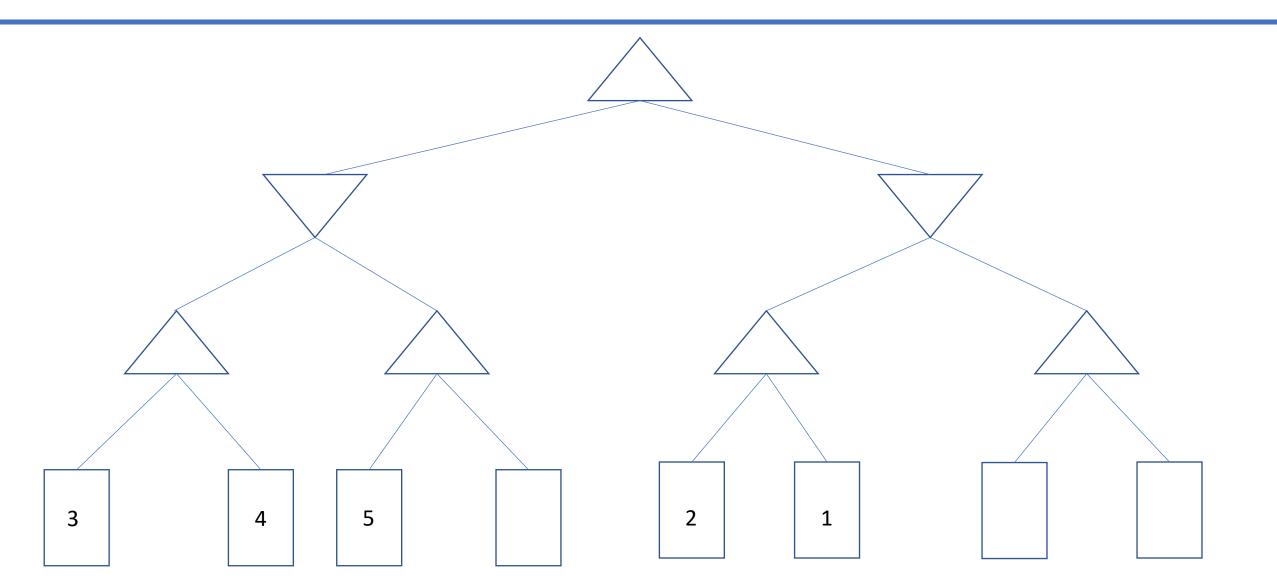
Alpha-Beta Pruning

- General configuration (MIN version)
 - We're computing the MIN-VALUE at some node n
 - We're looping over n's children
 - n's estimate of the childrens' min is dropping
 - Who cares about n's value? MAX
 - Let a be the best value that MAX can get at any choice point along the current path from the root
 - If *n* becomes worse than *a*, MAX will avoid it, so we can stop considering *n*'s other children (it's already bad enough that it won't be played)

MAX version is symmetric



Alpha-Beta Pruning





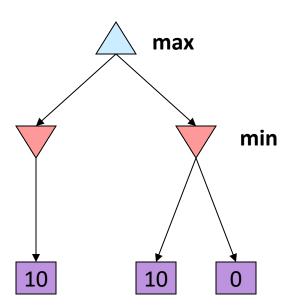
Alpha-Beta Pruning Properties

- This pruning has no effect on minimax value computed for the root!
- Values of intermediate nodes might be wrong
 - Important: children of the root may have the wrong value
 - So the most naïve version won't let you do action selection
- Good child ordering improves effectiveness of pruning
- With "perfect ordering":
 - Time complexity drops to O(b^{m/2})
 - Doubles solvable depth!

 - Full search of, e.g. chess, is still hopeless...







Alpha Beta Quiz

