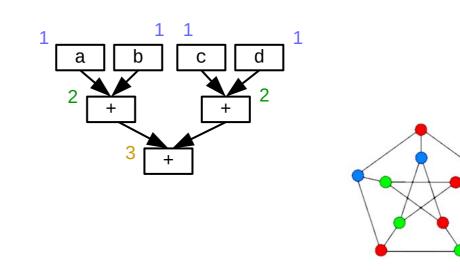
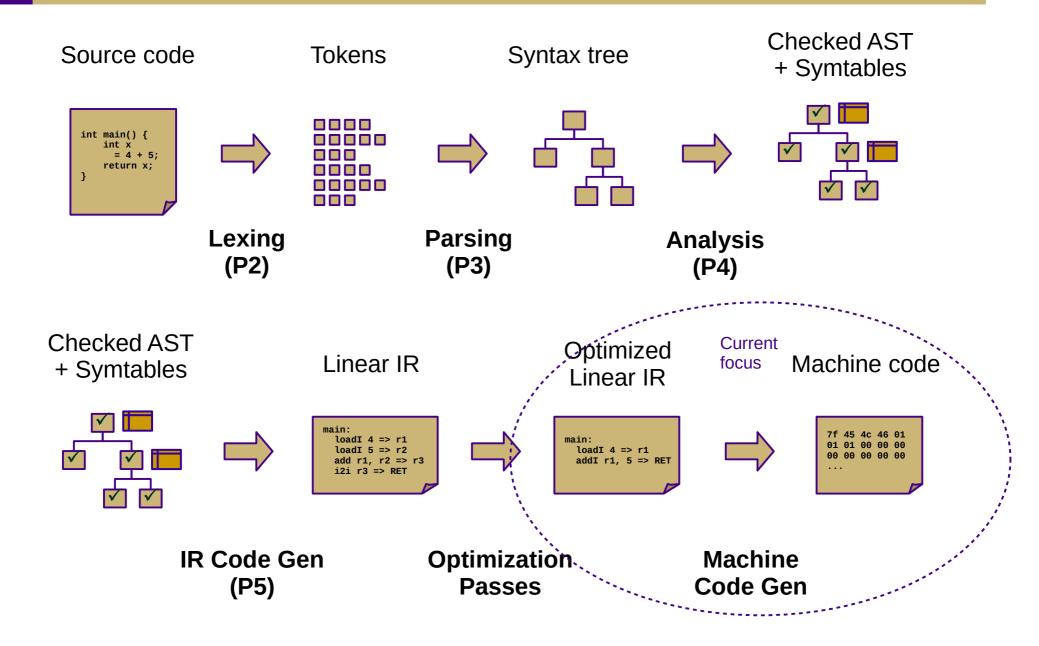
CS 432 Fall 2023

Mike Lam, Professor



Register Allocation

Compilers



Machine Code Gen (Ch. 11-13)

- Translate from (usually linear) IR to machine code
 - Often, compilers will just emit assembly
 - Use built-in system assembler and linker to create final executable
- Issues:
 - Translation from IR instructions to machine code instructions
 - Instruction selection (Ch. 11) example in y86.c provided w/ P5
 - Arrangement of machine code instructions for optimal pipelining
 - Instruction scheduling (Ch. 12) algorithm next week; no implementation
 - Assignment of registers to minimize memory accesses
 - Register allocation (Ch. 13) primary focus of P5

Instruction Selection

- Choose machine code instructions to replace IR
 - Complexity is highly dependent on target architecture
 - CISC provides more options than RISC (e.g., x86 vs. ARM)
 - Tradeoff: (possible) performance improvement vs. compiler complexity
- Algorithms:
 - Treewalk routine (similar to P4)
 - Tree-pattern matching / tiling (variant implemented in y86.c in P5)

$$d = a + c^{*}4 + 8 \implies \text{multI c, } 4 \Rightarrow t1$$

$$add a, t1 \Rightarrow t2$$

$$add I t2, 8 \Rightarrow d$$

$$\text{MultI c, } 4 \Rightarrow t1$$

$$add \% rax, \% rdi$$

$$add \% s8, \% rdi$$

$$\text{leaq } 0x8(\% rax,\% rcx, 4), \% rdx$$

$$\text{Source Language}$$

$$\text{Intermediate}_{\text{Representation (IR)}}$$

$$\text{Target Language}$$

%rcy %rdi

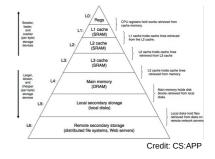
mov

Instruction Scheduling

- Modern CPUs expose many opportunities for optimization
 - Some instructions require fewer cycles
 - Instruction pipelining
 - Branch prediction and speculative execution
 - Multicore shared-memory processors
- Scheduling: re-order instructions to improve speed
 - Must not modify program semantics
 - Maximize utilization of CPU and memory resources
 - Main algorithm: list scheduling (next week!)

Register Allocation

- Maximizing register use is very important
 - Registers are the lowest-latency memory locations
 - Issue: limited number of registers
 - Everything not in registers must be stored in cache or main memory
 - Need to reduce the # of registers used to match the target system
 - Program using *n* registers => Program using *m* registers (n >> m)
- Allocation vs. assignment
 - Allocation: map a virtual register space to a physical register space
 - This is hard (NP-complete for any realistic situation)
 - Assignment: map a valid allocation to actual register names
 - This is easy (linear or polynomial)



Question

• Which virtual registers should be allocated to "real" physical registers and which must be allocated elsewhere?

```
add:
  loadAI [bp+16] => r0
  loadAI [bp+24] => r1
  add r0, r1 => r2
  i2i r2 => ret
  return
main:
  loadI 3 => r3
  storeAI r3 => [bp-8]
  loadAI [bp-8] => r4
  loadI 2 => r5
  param r5
  param r4
  call add
  i2i ret => r6
  i2i r6 => ret
  return
```

Local Allocation

- Top-down local register allocation
 - Compute a priority for each virtual register
 - Frequency of access to that register
 - Sort by priority, highest to lowest
 - Assign registers in order, highest priority first
 - Rewrite the code
- General idea: prioritize most-often-accessed virtual registers
 - Allocate to physical registers in priority order
 - Very simple to implement
 - Static per-block allocations are not always optimal
 - Access patterns may change throughout block
 - Especially in SSA form where registers aren't often re-used

Local Allocation

- Bottom-up local register allocation
 - Scan each block instruction-by-instruction
 - Essentially, simulate running the program
 - Maintain physical-to-virtual register mapping ("Name")
 - Initialize registers to empty ("INVALID") at beginning of block
 - For each instruction:
 - Assign virtual registers to physical registers
 - Ensure operands are in physical registers (load them if not)
 - Greedy algorithm: choose best allocation available at each instruction
 - Track next reference and free physical registers as soon as possible



Suppose we have three physical registers:

```
Name[R0] = INVALID r^{-} INVALID r^{-} INVALID
Name[R1] = INVALID r^{-} INVALID
Name[R2] = INVALID
```

add: loadAI [bp+16] => r0 loadAI [bp+24] => r1 add r0, r1 => r2 i2i r2 => ret return



add: loadAI [bp+16] => <u>R0</u> loadAI [bp+24] => <u>R1</u> add <u>R0</u>, <u>R1</u> => <u>R0</u> i2i <u>R0</u> => ret return

Example

```
add:
add:
  loadAI [bp+16] => r0
                                             loadAI [bp+16] => R0
  loadAI [bp+24] => r1
                                             loadAI [bp+24] => R1
                                             add R0, R1 => R0
  add r0, r1 => r2
                                             i2i R0 => ret
  i2i r2 => ret
                                             return
  return
                                           main:
main:
  loadI 3 => r3
                                             loadI 3 => R0
                                             storeAI R0 => [bp-8]
  storeAI r3 => [bp-8]
                                             loadAI [bp-8] => R0
  loadAI [bp-8] => r4
                                             loadI 2 => R1
  loadI 2 => r5
                                             param R1
  param r5
                                             param R0
  param r4
  call add
                                             call add
                                             i2i ret => R0
  i2i ret => r6
                                             i2i R0 => ret
  i2i r6 => ret
  return
```

return

Only needed two physical registers for this example!

Example

```
gcd:
l1:
  loadAI [bp+24] => r0
  loadI 1 => r1
  cmp GE r0, r1 => r2
 cbr r2 => l2, l3
12:
  loadAI [bp+24] => r3
  loadI 0 => r4
  store r3 => [r4]
  loadAI [bp+16] => r5
  loadAI [bp+24] => r6
  div r5, r6 => r7
  mult r6, r7 => r8
  sub r5, r8 => r9
  storeAI r9 => [bp+24]
  loadI 0 => r10
  load [r10] => r11
  storeAI r11 => [bp+16]
  jump l1
13:
  loadAI [bp+16] => r12
  i2i r12 => ret
  return
```

```
gcd:
l1:
  loadAI [bp+24] => R0
  loadI 1 => R1
 cmp_GE R0, R1 => R0
 cbr R0 => l2, l3
l2:
  loadAI [bp+24] => R0
  loadI 0 => R1
  store R0 => [R1]
  loadAI [bp+16] => R0
  loadAI [bp+24] R1
  div R0, B1 = R2
 mult R1, R2 > R1
  sub R0, R1 => R0
  storeAI R0 => [bp+24]
  loadI 0 => R0
  load [R0] => R0
  storeAI R0 => [bp+16]
  jump l1
13:
  loadAI [bp+16] => R0
  i2i R0 => ret
  return
```

What if we only had two physical registers?

Spilling

- If no physical registers are free, spill one!
 - Store its value to memory and re-load it later
 - For optimal results, spill register that will be accessed the furthest in the future
 - Store Next[pr] for this purpose or just re-calculate when needed
- This is the hardest part of P5 (leave it for last!)
 - Allocate slot in stack frame for each spilled register
 - It's essentially a new local variable
 - Track the offset for each virtual register
 - Emit load/store instructions as needed
 - Significant helper code is provided!

Bottom-up local register allocation

```
qcd:
l1:
  loadAI [bp+24] => r0
 loadI 1 => r1
 cmp_GE r0, r1 => r2
 cbr r2 => l2, l3
l2:
  loadAI [bp+24] => r3
  loadI 0 => r4
  store r3 => [r4]
  loadAI [bp+16] => r5
  loadAI [bp+24] => r6
 div r5, r6 => r7
 mult r6, r7 => r8
  sub r5, r8 => r9
  storeAI r9 => [bp+24]
  loadI 0 => r10
 load [r10] => r11
 storeAI r11 => [bp+16]
 jump l1
13:
  loadAI [bp+16] => r12
 i2i r12 => ret
 return
```

```
gcd:
11:
  loadAI [bp+24] => R0
  loadI 1 => R1
  cmp_GE R0, R1 => R0
 cbr R0 => l2, l3
12:
  loadAI [bp+24] => R0
  loadI 0 => R1
  store R0 => [R1]
  loadAI [bp+16] => R0
  loadAI [bp+24] => R1
  div R0, R1 => ???
  mult R1, ??? => R1
  sub R0, R1 => R0
  storeAI R0 => [bp+24]
  loadI 0 => R0
  load [R0] => R0
  storeAI R0 => [bp+16]
  jump l1
13:
  loadAI [bp+16] => R0
  i2i R0 => ret
  return
```

Bottom-up local register allocation

```
gcd:
l1:
  loadAI [bp+24] => r0
 loadI 1 => r1
 cmp_GE r0, r1 => r2
 cbr r2 => l2, l3
l2:
  loadAI [bp+24] => r3
  loadI 0 => r4
 store r3 => [r4]
  loadAI [bp+16] => r5
  loadAI [bp+24] => r6
 div r5, r6 => r7
 mult r6, r7 => r8
  sub r5, r8 => r9
  storeAI r9 => [bp+24]
  loadI 0 => r10
 load [r10] => r11
 storeAI r11 => [bp+16]
 jump l1
13:
  loadAI [bp+16] => r12
 i2i r12 => ret
 return
```

```
qcd:
l1:
  loadAI [bp+24] => R0
  loadI 1 => R1
 cmp_GE R0, R1 => R0
 cbr R0 => l2, l3
l2:
  loadAI [bp+24] => R0
  loadI 0 => R1
  store R0 => [R1]
  loadAI [bp+16] => R0
  loadAI [bp+24] => R1
  storeAI R0 => [bp-8] // store r5
  div R0, R1 => R0
 mult R1, R0 => R1
  loadAI [bp-8] => R0 // load r5
  sub R0, R1 => R0
  storeAI R0 => [bp+24]
  loadI 0 => R0
  load [R0] => R0
  storeAI R0 => [bp+16]
  jump l1
13:
  loadAI [bp+16] => R0
  i2i R0 => ret
  return
```

Full algorithm

for each instruction *i* in program:

for each vr read in i:
 pr = Ensure(vr)
 replace vr with pr in i
 if vr is not needed after i then free pr

for each vr written in i:

pr = Allocate(vr)
replace vr with pr in i

Ensure(vr): if vr is in pr: return pr else: pr = Allocate(vr) emit load from vr return pr

Allocate(vr): if *pr* is available: return *pr* else: find furthest-used *pr* to spill emit spill for *pr* return *pr*

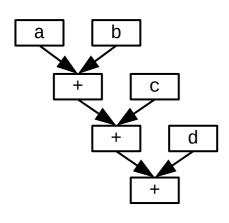
Textbook vs. reference compiler

- Textbook algorithm uses a stack to store free registers
 - Must remember to add registers to stack when freeing them
 - O(1) access to a free register if one is available
- Reference compiler scans physical registers for first free one
 - O(k) where k is number of physical registers, which is essentially a small constant
 - Only need Name[pr]
 - *pr* is free if Name[*pr*] == INVALID

TEXTBOOK:	REFERENCE:
loadI 1 => R0	loadI 1 => R0
loadI 2 => R1	loadI 2 => R1
add R0, R1 => R1	add R0, R1 => R0

Expression evaluation

- How many registers does it take to evaluate an arbitrary expression without any spilling?
 - Is there an easy way to determine this?

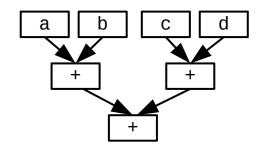


For example:

a + b + c + d

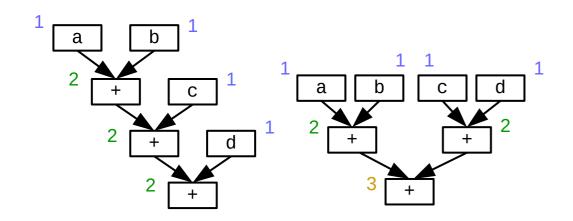
VS.

(a+b) + (c+d)



Expression evaluation

- How many registers does it take to evaluate an an arbitrary expression without any spilling?
 - Examine the expression tree (e.g., parse tree)
 - Calculate the Strahler number:
 - If the node is a leaf (has no children), its Strahler number is one.
 - If the node has one child with Strahler number i, and all other children have Strahler numbers less than i, then the Strahler number of the node is i.
 - If the node has two or more children with Strahler number i, and no children with greater number, then the Strahler number of the node is i + 1.



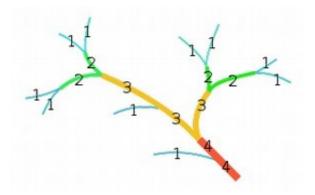


Image from https://en.wikipedia.org/wiki/Strahler_number

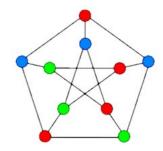
Systems design tradeoff

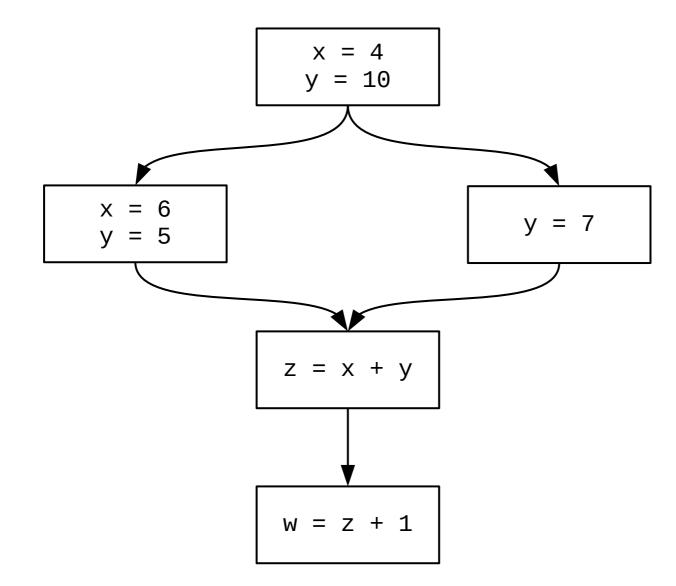
- Parallelism vs. register pressure
 - Balanced trees provide more parallelism and (as we'll see next week) better pipelining
 - However, more spills => worse performance
 - Unbalanced trees require fewer registers
 - Fewer spills => better performance
 - However, fewer opportunities for parallelism and pipelining
 - Usually the parallelism is worth the increased register pressure
 - Especially in the presence of forwarding and robust caches

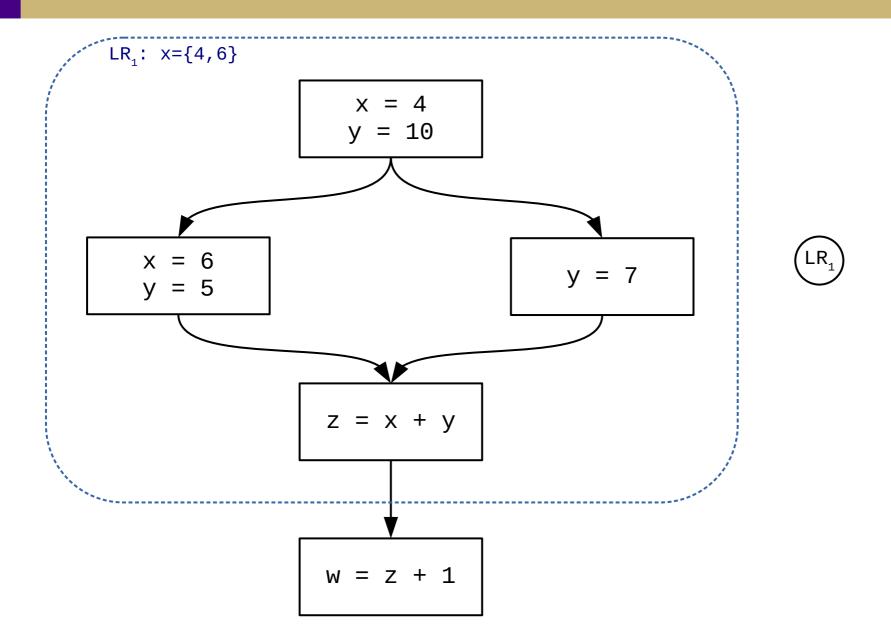
Local vs. global allocation

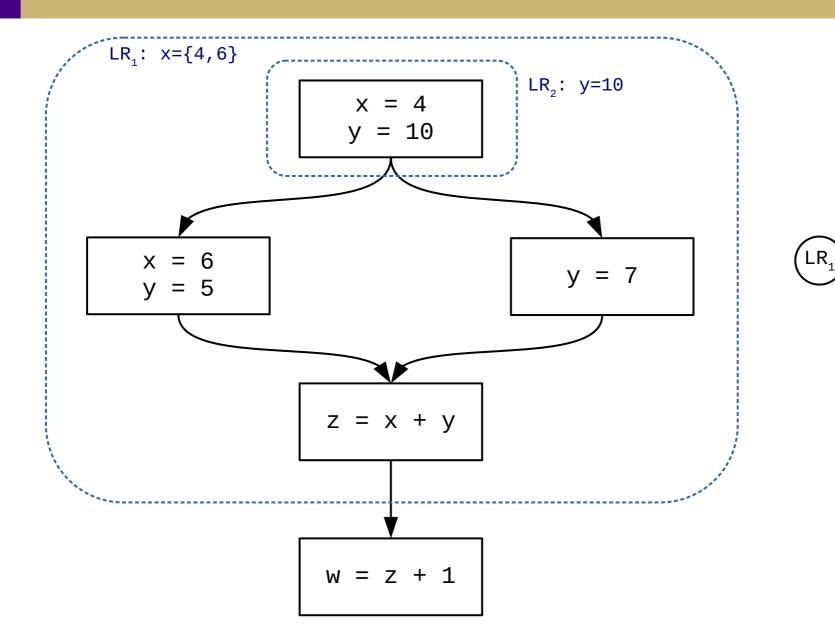
- Local allocation handles each basic block separately
 - Will miss inter-block dependencies
- Global allocation handles all basic blocks in a procedure
 - Does NOT consider inter-procedural dependencies
 - This is why calling conventions are important
 - I.e., caller-save vs. callee-save and return value
- Decaf project
 - Because we used SSA in P4 and always load/store to memory, no virtual registers will be live at the entrance or exit of any block (so no inter-block dependencies)
 - Thus, we can use local register allocation in P5

- Discover global live ranges of related uses and definitions
 - For each use, any reaching definitions must be in the same range
 - For each definition, any reachable uses must be in the same range
 - Simple disjoint-set union-find algorithm over SSA form
- Build interference graph
 - Node for each live range and edges between interfering live ranges
- Attempt to compute graph *k*-coloring
 - *k* is the number of physical registers
 - Greedy algorithm: order the colors (registers)
 - For each vertex, choose smallest color not shared by neighbors
 - If successful, done!
 - If not successful, spill some values and try again
 - Need a robust way to pick which values to spill
 - Alternatively, split live ranges at carefully-chosen points

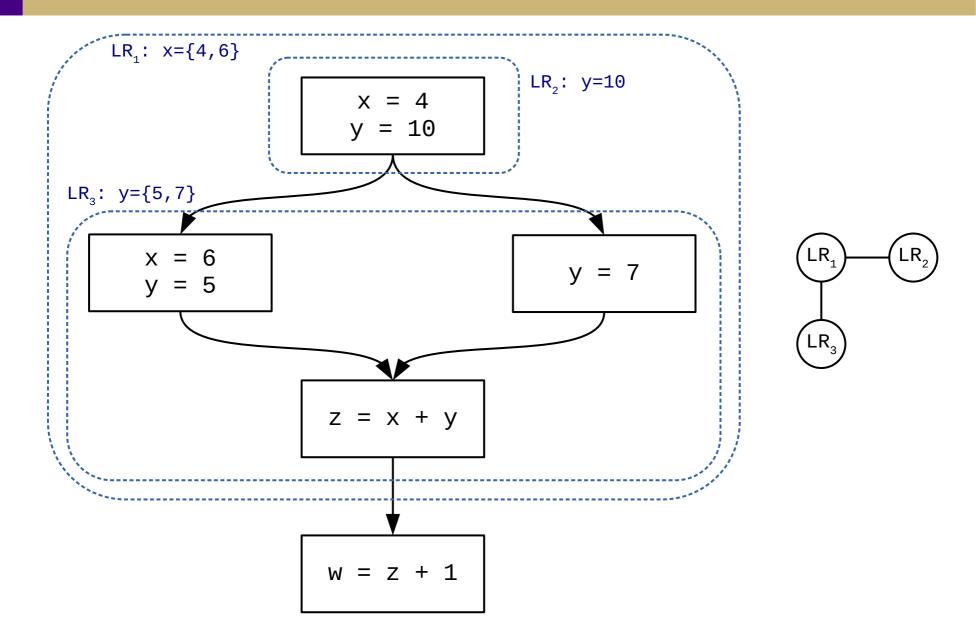


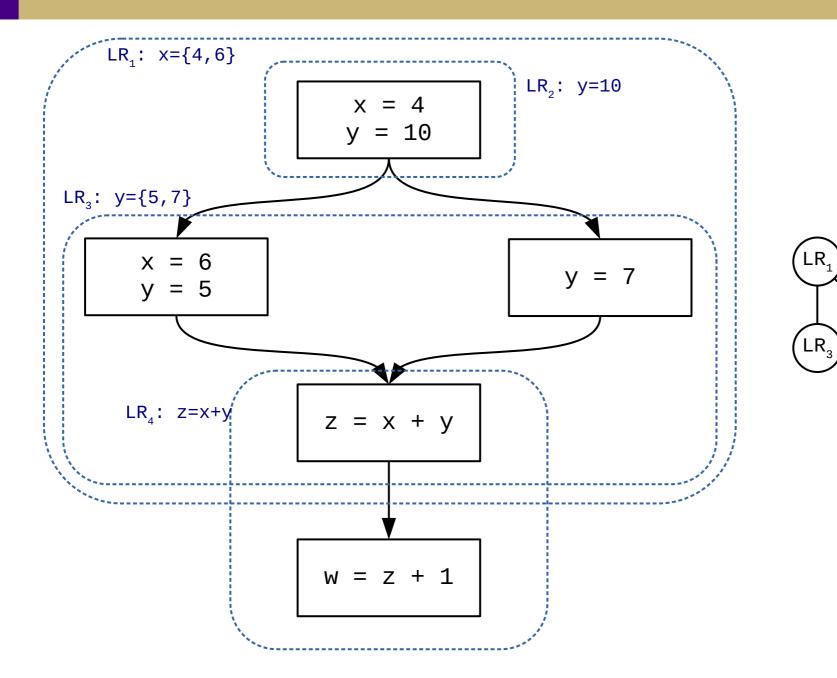






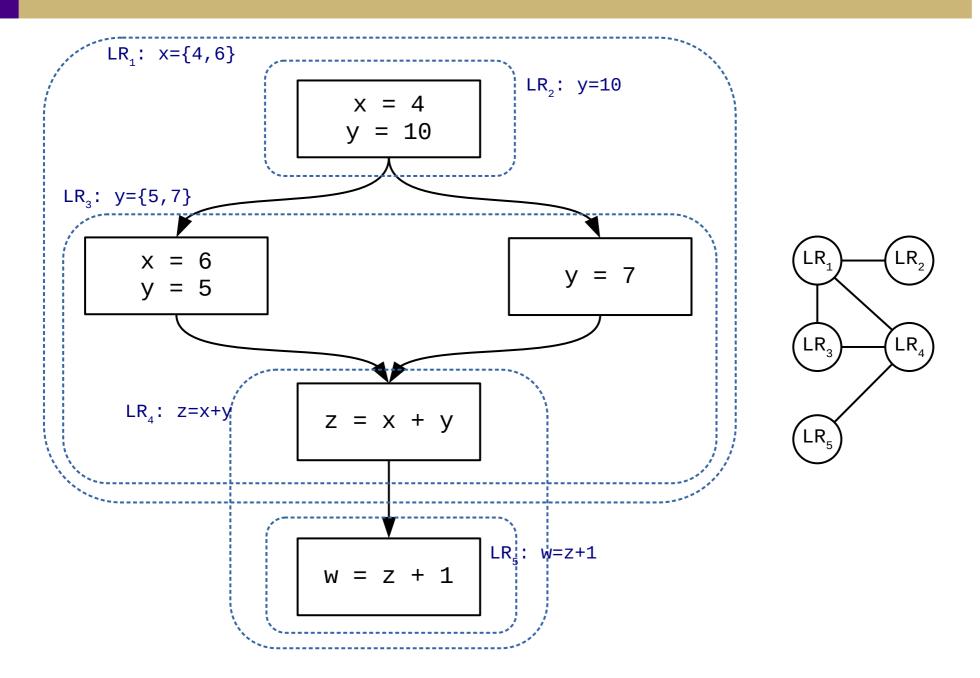
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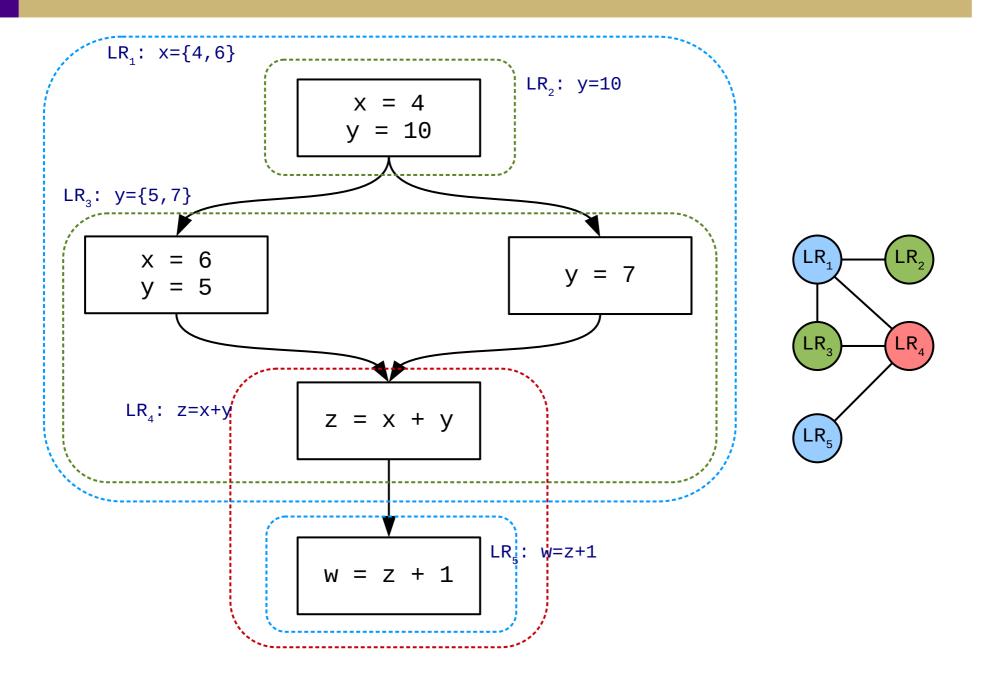




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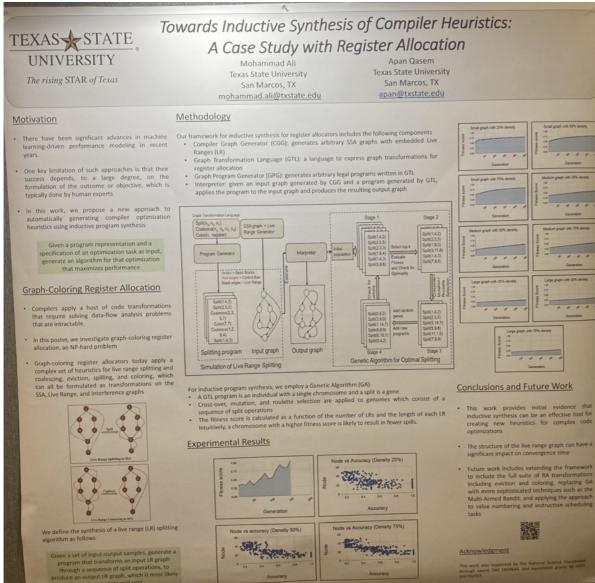
LR₄





SC23 poster

to minimize spill cost





Denver, CO i am hpc.