CS 432 Fall 2023

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(AN UNMATCHED LEFT PARENTHESIS CREATES AN UNRESOLVED TENSION THAT WILL STAY WITH YOU ALL DAY.

https://xkcd.com/859/

Bottom-Up (LR) Parsing

Compilation



Overview

- Two general parsing approaches
 - Top-down: begin with start symbol (root of parse tree), and gradually expand non-terminals
 - Bottom-up: begin with terminals (leaves of parse tree), and gradually connect using non-terminals



Shift-Reduce Parsing

- Top-down (LL) parsers
 - Left-to-right scan, Leftmost derivation
 - Recursive routines, one per non-terminal (*recursive descent*)
 - Implicit stack (system call stack)
 - Requires more restrictive grammars
 - Simpler to understand and possible to hand-code
- Bottom-up (LR) parsers
 - Left-to-right scan, (reverse) Rightmost derivation
 - "Shift"/push terminals and non-terminals onto a stack
 - "Reduce"/pop to replace *handles* with non-terminals
 - Less restrictive grammars
 - Harder to understand and nearly always auto-generated; very efficient!

Shift-Reduce Parsing

• V = E

• V = E +

- shift '+'

- shift 'c'

• V = E + c

• $V = \underline{E} + V$

• V = E

• A

- reduce (V \rightarrow c)

- reduce (E \rightarrow E + V)

- reduce (A \rightarrow V = E)

- - shift 'a'
- <u>a</u>
 - reduce (V → a)
- V
 - shift '='
- V =
 - shift 'b'
- V = <u>b</u>
 - reduce (V \rightarrow b)
- $V = \underline{V}$
 - reduce (E \rightarrow V) accept

(handles are underlined)

shift = push, reduce = popN

- Α Ε + Ε а С h $A \rightarrow V = E$ $E \rightarrow E + V$ $V \rightarrow a \mid b \mid c$
 - "a = b + c"

LR Parsing

- LR(1) grammars and parsers
 - Left-to-right scan of the input string
 - Rightmost derivation
 - **<u>1</u> symbol** of lookahead
 - Less restricted form of context-free grammar
 - Support for most language features
 - Efficient parsing



LR Parser Variants

- LR(k) multiple lookaheads (not necessary)
- LR(1) single lookahead (EAC covers this!)
 - Very general and very powerful
 - Lots of item sets; tedious to construct by hand
 - Overkill for most practical languages
- LALR(1) special case of LR(1) that merges some states
 - Less powerful, but easier to manage
- **SLR(1)** special case of LR(1) w/o explicit lookahead (*Dragon book covers this!*)
 - Uses FOLLOW sets to disambiguate
 - Even less powerful, but much easier to understand
 - Slightly counterintuitive: all LR(1) languages have SLR(1) grammars
 - So SLR(1) is sufficiently general for our purposes
 - Use LR(0) item sets and generate SLR(1) ACTION/GOTO tables
- LR(0) no lookahead
 - Severely restricted; most "interesting" grammars aren't LR(0)

LR Parsing

- Creating an LR parser (pushdown automaton)
 - Build item sets from grammar productions
 - An item uses a dot (•) to represent parser status: "A \rightarrow a S b"
 - Dots on the left end: "possibilities"
 - Dots in the middle: "partially-complete"
 - Dots on the right end: "complete"
 - Item sets represent multiple parser states (build by taking closure)
 - Similar to NFA state collections in subset construction
 - Build **ACTION / GOTO** tables
 - Encodes stack and transition decisions (like δ in FA)
 - **ACTION**(state, terminal) = { *shift/push*, *reduce/pop*, *accept* }
 - **GOTO**(state, non-terminal) = state

LR(0) Item Sets

 LR(0) item sets and automaton 	$S \rightarrow a S b$
 Start with an item representing "• S" or "S' → • S" The latter is an augmented grammar 	a b
 The Dragon book uses it; the online tool doesn't Take the closure to add more states if the dot lies immediately to the left of a non-terminal 	$I_0: \bullet S$ $S \rightarrow \bullet a S b$ $S \rightarrow \bullet a b$
 (Non-kernel items, denoted here in blue) Form new sets by "moving the dot" (and take the closure) 	I ₁ : S •
 Convert to finite automaton for recognizing handles by adding transitions Each set becomes a state "Moving the dot" = state transition + stack push 	$I_{2}: S \rightarrow a \cdot S b$ $S \rightarrow a \cdot b$ $S \rightarrow a \cdot b$ $S \rightarrow a S b$ $S \rightarrow a b$
	$I_3: S \rightarrow a S \bullet b$
$\begin{array}{c c} \bullet S \\ S \rightarrow \bullet a S b \\ S \rightarrow \bullet a b \end{array} \qquad a \\ 2 \\ 2 \\ S \rightarrow a S \bullet b \\ S \rightarrow a S \bullet b \\ S \rightarrow a S b \bullet \\ S \rightarrow a S \rightarrow \\ S \rightarrow a S b \bullet \\ S \rightarrow a$	I_4 : $S \rightarrow a b \bullet$
$ \begin{array}{c} S \rightarrow a \cdot S b \\ S \rightarrow a \cdot b \\ S \rightarrow \cdot a S b \\ S \rightarrow \cdot a b \end{array} $	I_5 : $S \rightarrow a \ S \ b \bullet$

SLR(1) Tables

- Create ACTION and GOTO tables
 - For each item set i
 - If an item matches $\mathbf{A} \rightarrow \mathbf{\beta} \bullet \mathbf{c} \mathbf{y}$
 - ACTION(i, c) = "shift" to corresponding item set ("move the dot")
 - If an item matches $A \rightarrow \beta$
 - ACTION(i, x) = "reduce A $\rightarrow \beta$ " for all x in FOLLOW(A) ("backtrack in FA")
 - If an item matches $A \rightarrow \beta \bullet B \gamma$
 - **GOTO**(i, B) = corresponding item set ("move the dot")
 - ACTION({S •}, \$) = "accept"
 - Any empty ACTION entry = "error" (usually left blank)

SLR(1) Parsing

- Push state 0 onto the stack
- Repeat until next action is accept or error:
 - Look up next action in **ACTION** table
 - Row is the current state (top of stack)
 - Column is the next input (terminal or \$) s
 - If action is shift(s):
 - **Push** state s onto stack
 - Consume one token from input
 - If action is reduce ($A \rightarrow \beta$):
 - **Pop** one state for each terminal or non-terminal in β
 - Look up next state in GOTO table and push it onto the stack
 - Row is the current state (top of stack, *after* popping β)
 - Column is **A** (newly-reduced non-terminal)



Figure 4.35: Model of an LR parser $% \left({{{\rm{A}}_{\rm{B}}} \right)$

Example







Example

 $S \rightarrow a S b$ | a b

GOTO ACTION State \$ Sa b 0 shift(2) 1 1 accept 2 shift(2) 3 shift(4) 3 shift(5) 4 $reduce(S \rightarrow a b)$ $reduce(S \rightarrow a b)$ $reduce(S \rightarrow a S b) \quad reduce(S \rightarrow a S b)$ 5

Parsing for "a a b b":

(Dragon Book version)

<u>Sta</u>	<u>ack</u>			<u>Symbols</u>	Inpu	<u>ut</u>	<u>Action</u>
\$ 0 \$ 0 \$ 0	9 9 2 9 2	2		\$ \$ a \$ a a	a a b b a b b b b	\$ \$ \$	shift(2) shift(2) shift(4)
\$ 0 \$ 0) 2) 2	2 3	4	\$ a a b \$ a S	b b	\$ \$	reduce(S → a b) shift(5)
\$ 0 \$ 0) 2) 1	3	5	\$ a S b \$ S		\$ \$	reduce(S \rightarrow a S b) accept

Example

 $S \rightarrow a S b$ | a b

			AC	GOTO	
_	State	a	ь	S	S
	0	shift(2)			1
	1			accept	
	2	shift(2)	shift(4)		3
	3		shift(5)		
	4		$reduce(S \rightarrow a b)$	$reduce(S \longrightarrow \mathtt{a} \mathtt{b})$	
	5		$reduce(S \rightarrow a S b)$	$reduce(S \rightarrow a \ S \ b)$	
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Parsing for "a a b b":

(cleaner version w/ goto)

<u>Stack</u>	<u>Input</u>	<u>Action</u>	<u>Goto</u>
<u>0</u>	<u>a</u> a b b \$	shift(2)	-
0 <u>2</u>	<u>a</u> b b \$	shift(2)	-
02 <u>2</u>	<u>b</u> b\$	shift(4)	-
0 2 2 <u>4</u>	<u>b</u> \$	reduce $(\hat{S} \rightarrow a b)$	3
02 <u>3</u>	<u>b</u> \$	shift(5)	-
023 <u>5</u>	<u>\$</u>	reduce $(S \rightarrow a S b)$	1
0 <u>1</u>	<u>\$</u>	accept	

LR Conflicts

- Shift/reduce
 - Can be resolved by always shifting or by grammar modification
- Reduce/reduce
 - Requires grammar modification to fix

Shift/reduce conflict in LR(0)

Observation: none of these languages are LL(1) either!

A -> x A x A ->

Shift/reduce conflict (all LR)

A -> B | C B -> x C -> x

Reduce/reduce conflict (all LR)