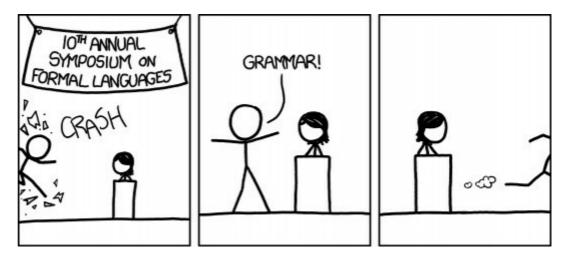
CS 432 Fall 2018

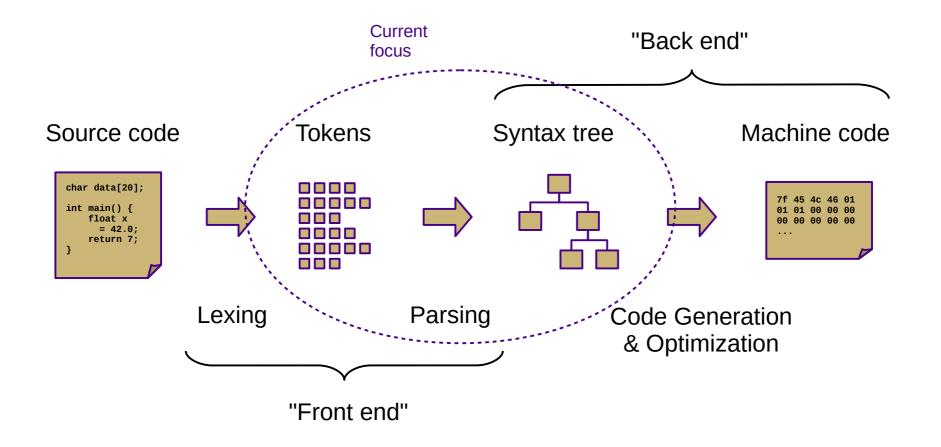
Mike Lam, Professor



[audience looks around] "What just happened?" "There must be some context we're missing."

Context-free Grammars

Compilation



Overview

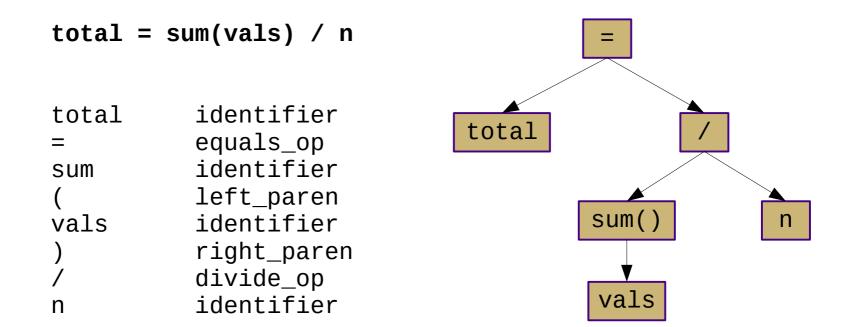
- General programming language topics
 - Syntax (what a program looks like)
 - Semantics (what a program means)
 - Implementation (how a program executes)



- Textbook: "the form of [a language's] expressions, statements, and program units."
 - In other words, the **form** or **structure** of the code
- Goals of syntax analysis:
 - Checking for program validity or correctness
 - Facilitate translation (compiler) or execution (interpreter) of a program

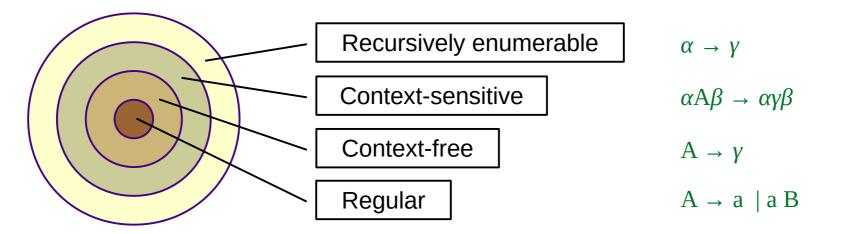
Syntax Analysis

- Tokens have no structure
 - No inherent relationship between each other
 - Need a way to describe hierarchy in a way that is closer to the semantics of the language



Languages

Chomsky Hierarchy of Languages



NOTE: Greek letters (α , β , γ) indicate arbitrary strings of terminals and/or non-terminals

- Regular languages are not sufficient to describe programming languages
 - Core issue: finite DFAs can't "count:" no way to express $a^m b^n$ where n = f(m)
 - Consider the language of all matched parentheses $(n)^n$
 - How can we solve this to make it feasible to write a compiler?

Add memory! (and move up the language hierarchy)

Syntax Analysis

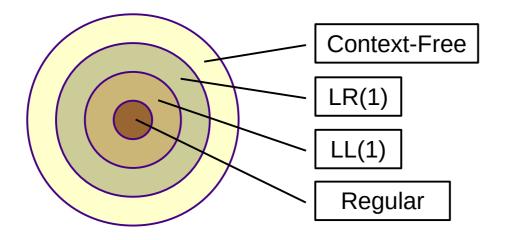
Context-free language

- More expressive than regular languages
- Encodes hierarchy and structure of language tokens
 - Usually represented using a tree
- Described by *context-free grammars*
 - Recursive description of the language's form
 - Usually written in Backus-Naur Form
- Recognized by *pushdown automata*
 - Two major approaches: top-down and bottom-up
 - Next two weeks
- Provide ways to control *ambiguity*, *associativity*, and *precedence* in a language

- A context-free grammar is a 4-tuple (T, NT, S, P)
 - T: set of terminal symbols (tokens)
 - NT: set of nonterminal symbols
 - S: start symbol (S ϵ NT)
 - P: set of productions or rules:

Example:

$$\begin{array}{cccccccccc} S & \rightarrow & X & S & X \\ S & \rightarrow & Y \end{array}$$



Context-Free Hierarchy

• Non-terminals vs. terminals

- Terminals are single tokens, non-terminals are aggregations
- One special non-terminal: the start symbol
- Production *rules*
 - Left hand side: single non-terminal
 - Right hand side: **sequence** of **terminals** and/or **non-terminals**
 - LHS can be replaced by the RHS (colloquially: "is composed of")
 - RHS can be empty (or " ϵ "), meaning it can be composed of nothing
- Sentence: a sequence of terminals
 - A sentence is a member of a language if and only if it can be derived using the language's grammar

- *Derivation*: a series of grammar-permitted transformations leading to a sentence
 - Begin with the grammars start symbol (a non-terminal)
 - Each transformation applies exactly one rule
 - Expand one non-terminal to a string of terminals and/or non-terminals
 - Each intermediate string of symbols is a *sentential form*
 - Leftmost vs. rightmost derivations
 - Which non-terminal do you expand first?
 - *Parse tree* represents a derivation in tree form (the sentence is the sequence of all leaf nodes)
 - Built from the top down during derivation
 - Final parse tree is called *complete* parse tree
 - For a compiler: represents a program, executed from the bottom up

- Backus-Naur Form: list of context-free grammar rules
 - Usually beginning with start symbol
 - Convention: non-terminals start with upper-case letters
 - Combine rules using "|" operator:

- Several formatting variants:

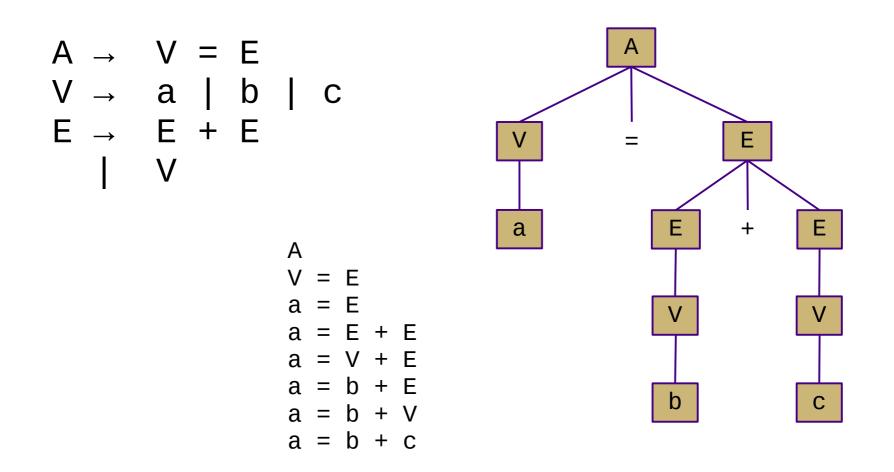
<Assign> ::=<Var> = <Expr>A \rightarrow V = E<Var> ::=a | b | cV \rightarrow a | b | c<Expr> ::=<Expr> + <Expr>E \rightarrow E + E|<Var>|V

Example

 Show the leftmost derivation and parse tree of the sentence "a = b + c" using this grammar:

Example

 Show the leftmost derivation and parse tree of the sentence "a = b + c" using this grammar:



Example

- Let's revisit the "matched parentheses" problem
 - Cannot write a regular expression for $\binom{n}{r}^{n}$
 - How about a context-free grammar?
 - First attempt:

$$\begin{array}{cccc} S & \rightarrow & \underline{(} & S & \underline{)} \\ S & \rightarrow & \epsilon \end{array}$$

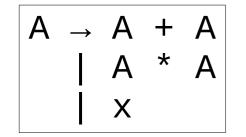
Use underlining to indicate literal terminals when ambiguous

- Second attempt:

What (if anything) is wrong with this:

Ambiguous Grammars

- An ambiguous grammar allows multiple derivations (and therefore parse trees) for the same sentence
 - The semantics may be similar, but there is a difference syntactically!
 - Example: if/then/else construct
 - It is important to be precise!
- Often can be eliminated by rewriting the grammar
 - Usually by making one or more rules more restrictive



Ambiguous (Associativity/Precedence)

$$\begin{array}{ccccccc} A & \rightarrow & B & | & C \\ B & \rightarrow & X & \\ C & \rightarrow & X & \end{array}$$

Ambiguous (Ad-hoc)

$$\begin{array}{cccc} A & \rightarrow & \text{ifthen} & A & \text{else} & A \\ & & & & \text{ifthen} & A \\ & & & & \text{stmt} \end{array}$$

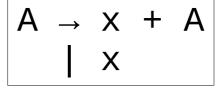
Ambiguous ("Dangling Else" Problem)

Operator Associativity

- Does x+y+z = (x+y)+z or x+(y+z)?
 - Former is left-associative
 - Latter is right-associative
- Closely related to recursion
 - Left-hand recursion \rightarrow left associativity
 - Right-hand recursion \rightarrow right associativity
- Sometimes enforced explicitly in a grammar
 - Different non-terminals on left- and right-hand sides of an operator
 - Sometimes just noted with annotations

$$\begin{array}{cccc} A \rightarrow A + X \\ I & X \end{array}$$

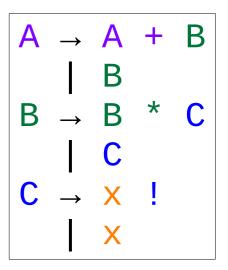
Left Associative



Right Associative

Operator Precedence

- Precedence determines the relative priority of operators
- Does x+y*z = (x+y)*z or x+(y*z)?
 - Former: "+" has higher precedence
 - Latter: "*" has higher precedence
- Sometimes enforced explicitly in a grammar
 - One non-terminal for each level of precedence
 - Each level contains references to the next level
 - Sometimes just noted with annotations
 - Same approach for unary and binary operators
 - For binary operators: left or right associativity?
 - For unary operators: prefix or postfix?
 - For unary operators: is repetition allowed?



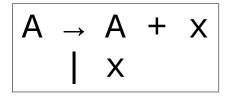
Precedence

- + (lowest)
- * (middle)
- ! (highest)

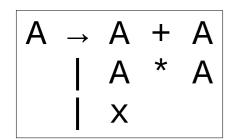
Grammar Examples

$$\begin{array}{cccc} A & \rightarrow & A & X \\ & & | & X \end{array}$$

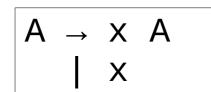
Left Recursive



Left Associative



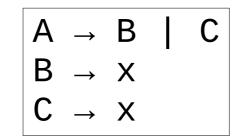
Ambiguous (Associativity/Precedence)



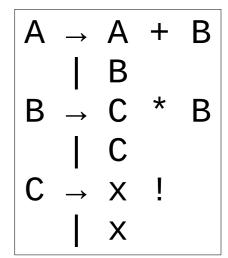
Right Recursive

$$\begin{vmatrix} A & \rightarrow & X & + & A \\ & | & X & & \end{vmatrix}$$

Right Associative



Ambiguous (Ad-hoc)



Associativity/Precedence + (lowest, left-associative) * (middle, right-associative) ! (highest, postfix unary)

Ambiguous ("Dangling Else" Problem)