# CS 432 <br> Fall 2017 

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## Bottom-Up (LR) Parsing

## Compilation



## Overview

- Two general parsing approaches
- Top-down: begin with start symbol (root of parse tree), and gradually expand non-terminals
- Bottom-up: begin with terminals (leaves of parse tree), and gradually connect using non-terminals



## Shift-Reduce Parsing

- Top-down (LL) parsers
- Left-to-right scan, Leftmost derivation
- Recursive routines, one per non-terminal (recursive descent)
- Implicit stack (system call stack)
- Requires more restrictive grammars
- Simpler to understand and possible to hand-code
- Bottom-up (LR) parsers
- Left-to-right scan, (reverse) Rightmost derivation
- "Shift"/push terminals and non-terminals onto a stack
- "Reduce"/pop to replace handles with non-terminals
- Less restrictive grammars
- Harder to understand and nearly always auto-generated
- Very efficient


## Shift-Reduce Parsing

- 
- shift 'a'
- $\underline{a}$
- reduce $(\mathrm{V} \rightarrow \mathrm{a})$
- V
- shift ' $=$ '
- $\mathrm{V}=$
- shift 'b'
- $\mathrm{V}=\underline{\mathrm{b}}$
- reduce $(\mathrm{V} \rightarrow \mathrm{b})$
- $\mathrm{V}=\underline{\mathrm{V}}$
- reduce $(E \rightarrow V)$
- $V=E$
- shift '+'
- $\mathrm{V}=\mathrm{E}+$
- shift 'c'
- $V=E+\underline{c}$
- reduce $(\mathrm{V} \rightarrow \mathrm{c})$
- $V=\underline{E+V}$
- reduce $(E \rightarrow E+V)$
- $\mathrm{V}=\mathrm{E}$
- reduce ( $\mathrm{V}=\mathrm{E}$ )
- A
- accept
shift $=$ push, reduce $=$ popN



## - Creating an LR parser (pushdown automaton)

- Build item sets ("canonical collections")
- An item uses a dot (•) to represent parser status: "A $\rightarrow \mathrm{a} \cdot \mathrm{S} \mathrm{b}$ "
- Dots on the left end: "possibilities"
- Dots in the middle: "partially-complete"
- Dots on the right end: "complete"
- Item sets represent closures of parser states
- Similar to NFA state collections in subset construction
- Build ACTION / GOTO tables
- Encodes stack and transition decisions (replaces $\delta$ in FA)
- ACTION(state, terminal) $=\{$ shift/push, reduce/pop, accept $\}$
- GOTO(state, non-terminal) = state


## LR Parsing

- Item sets ("canonical collections")
- Start with an item representing "•S"
- Form new sets by "moving the dot"
- Take the closure to add more states if the dot lies to the left of a non-terminal
- (Denoted here in green)
- Can be converted to an automaton
- Each set becomes a state
- "Moving the dot" = transition between states
- "Backtrack" when reducing


$$
\begin{gathered}
S \rightarrow a S b \\
\mid a b b
\end{gathered}
$$

$$
\mathrm{CC}_{0}: \quad \cdot \mathrm{S}
$$

$$
S \rightarrow \cdot a S b
$$

$$
\mathrm{s} \rightarrow \cdot \mathrm{a} b
$$

$\mathrm{CC}_{1}$ : $\quad \mathrm{S} \cdot$
$C_{2}: S \rightarrow a \cdot S b$
$S \rightarrow a \cdot b$
$S \rightarrow$ •a S b
$S \rightarrow \cdot a b$
$\mathrm{CC}_{3}: S \rightarrow \mathrm{a} S \cdot \mathrm{~b}$
$\mathrm{CC}_{4}: \mathrm{S} \rightarrow \mathrm{ab} \cdot$
$\mathrm{CC}_{5}: S \rightarrow$ a S b

- How much lookahead do we need?
- Depends on how complicated the grammar is
- LR(k) - multiple lookaheads (not necessary)
- LR(1) - single lookahead (our textbook covers this!)
- Very general and very powerful
- Lots of item sets; tedious to construct by hand
- LALR - special case of LR(1) that merges some states
- Less powerful, but easier to manage
- SLR - special case of LR(1) w/o explicit lookahead
- Uses FOLLOW sets to disambiguate
- Even less powerful, but much easier to understand
- LR(0) - no lookahead
- Severely restricted; most "interesting" grammars aren't LR(0)


## SLR Parsing

- Construct LR(0) item sets and automaton
- Keep track of transitions ("moving the dot")
- Create ACTION and GOTO tables
- For each item set i
- If an item matches $A \rightarrow \beta \cdot \mathbf{c} y$
- ACTION(i, c) = "shift" to corresponding item set ("move the dot")
- If an item matches $A \rightarrow \beta$ -
- ACTION( $\mathrm{i}, \mathrm{x}$ ) = "reduce $A \rightarrow \beta^{\prime \prime}$ for all $x$ in FOLLOW(A) ("backtrack in FA")
- If an item matches $A \rightarrow \beta$ - $\mathbf{B}$ y
- GOTO(i, B) = corresponding item set ("move the dot")
- ACTION(S', \$) = "accept"


## SLR parsing

## $S \rightarrow a S b$ <br> 1 a b

| State | ACTION |  |  | GOTO |
| :---: | :---: | :---: | :---: | :---: |
|  | a | b | \$ | $S$ |
| 0 | shift(2) |  |  | 1 |
| 1 |  |  | accept |  |
| 2 | shift(2) | $\operatorname{shift}(4)$ |  | 3 |
| 3 |  | shift(5) |  |  |
| 4 |  | reduce $(S \rightarrow \mathrm{a} \mathrm{b})$ | reduce( $S \rightarrow \mathrm{ab}$ ) |  |
| 5 |  | reduce $(S \rightarrow$ a $S$ b | reduce $(S \rightarrow \mathrm{a} S \mathrm{~b})$ |  |



## LR(1) parsing

## $S \rightarrow a S b$ <br> lab



## LR Conflicts

- Shift/reduce
- Can be resolved by always shifting or by grammar modification
- Reduce/reduce
- Requires grammar modification to fix

$$
\begin{aligned}
& \mathrm{A}->\mathrm{V}=\mathrm{E} \\
& \mathrm{E}->\mathrm{E}+\mathrm{V} \\
& \mathrm{E}->\mathrm{V} \\
& \mathrm{~V} \rightarrow \mathrm{a}|\mathrm{~b}| \mathrm{C}
\end{aligned}
$$

Shift/reduce conflict in LR(0)

$$
\begin{aligned}
& A->\times A \times \\
& A->
\end{aligned}
$$

Shift/reduce conflict (all LR)

$$
\begin{array}{lll|l}
A & -> & B & C \\
B & -> & x & \\
C & -> & x &
\end{array}
$$

Reduce/reduce conflict (all LR)

