

# CS 261

## Fall 2016

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# Combinational Circuits

# Quiz

- Match the gates with their truth tables and write the boolean function name



	0	1
0	0	1
1	1	1

0	1
1	0

	0	1
0	1	0
1	0	0

	0	1
0	0	0
1	0	1

	0	1
0	0	1
1	1	0

	0	1
0	1	1
1	1	0

# Logic gates

- Primary gates:



	0	1
0	0	1
1	1	1

OR



!	
0	1
1	0

NOT



	0	1
0	1	0
1	0	0

NOR



&	0	1
0	0	0
1	0	1

AND



^	0	1
0	0	1
1	1	0

XOR



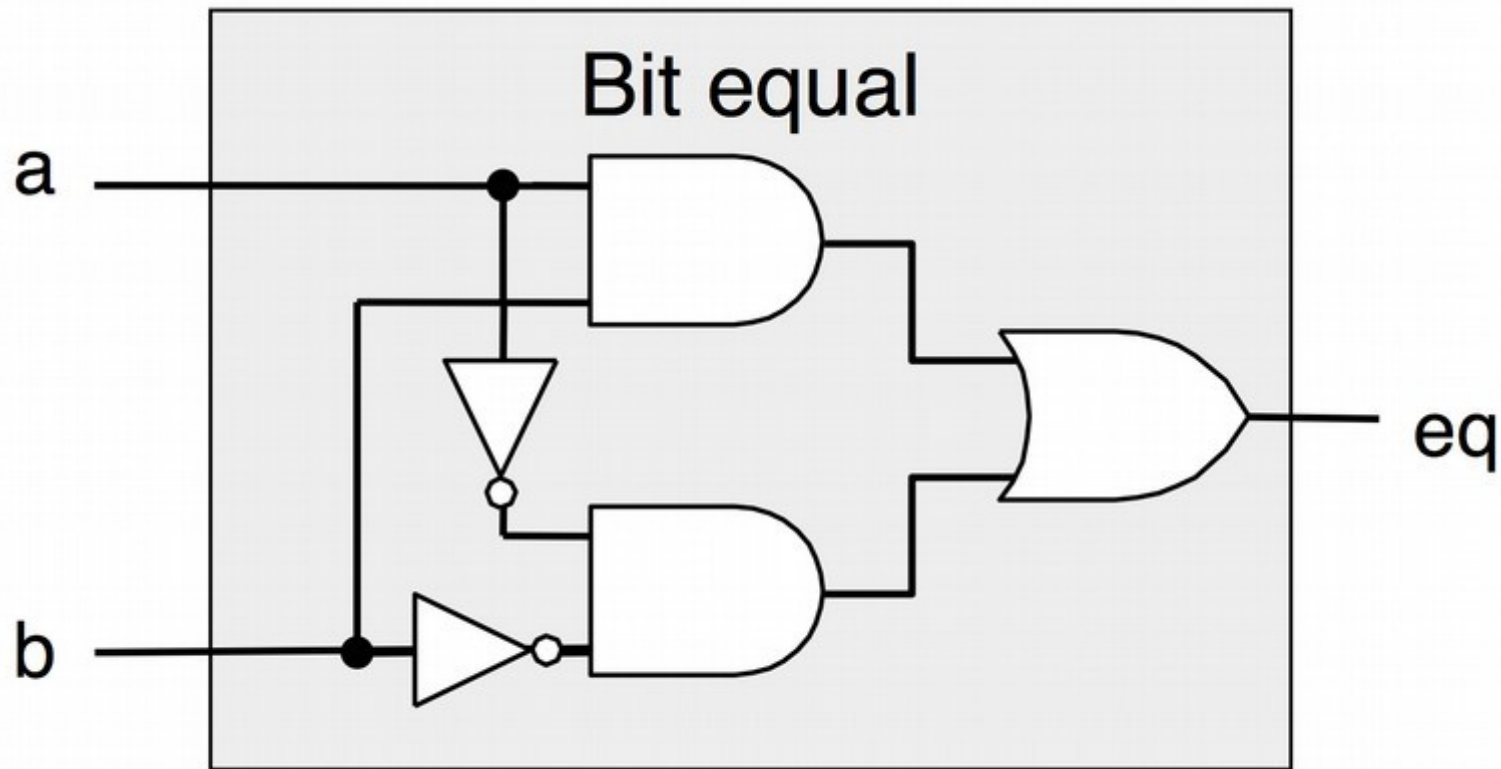
	0	1
0	1	1
1	1	0

NAND

# Circuits

- **Circuits** are formed by linking gates together
  - Inputs and outputs
    - Link output of one gate to input of another
    - Some gates have multiple inputs and/or outputs
  - **Combinational** circuits: outputs are a boolean function of inputs
    - Not time-dependent
    - Used for computation
  - **Sequential** circuits: output is dependent on previous inputs
    - Time-dependent
    - Used for memory

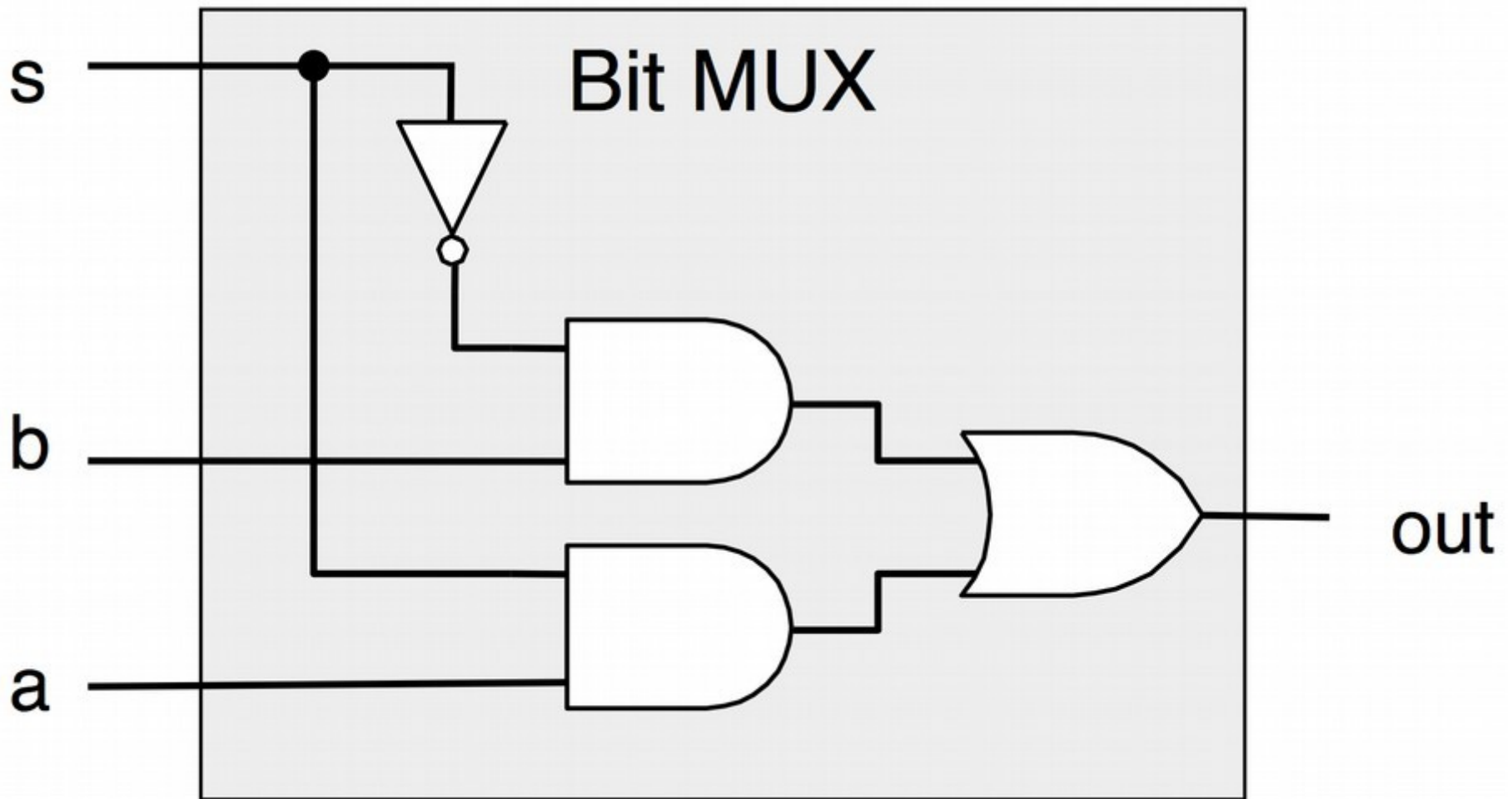
# Equality



$$a \text{ EQ } b = (a \ \& \ b) \ | \ (!a \ \& \ !b)$$

$$\text{EQ}(a, b) = \text{OR}(\text{AND}(a, b), \text{AND}(\text{NOT}(a), \text{NOT}(b)))$$

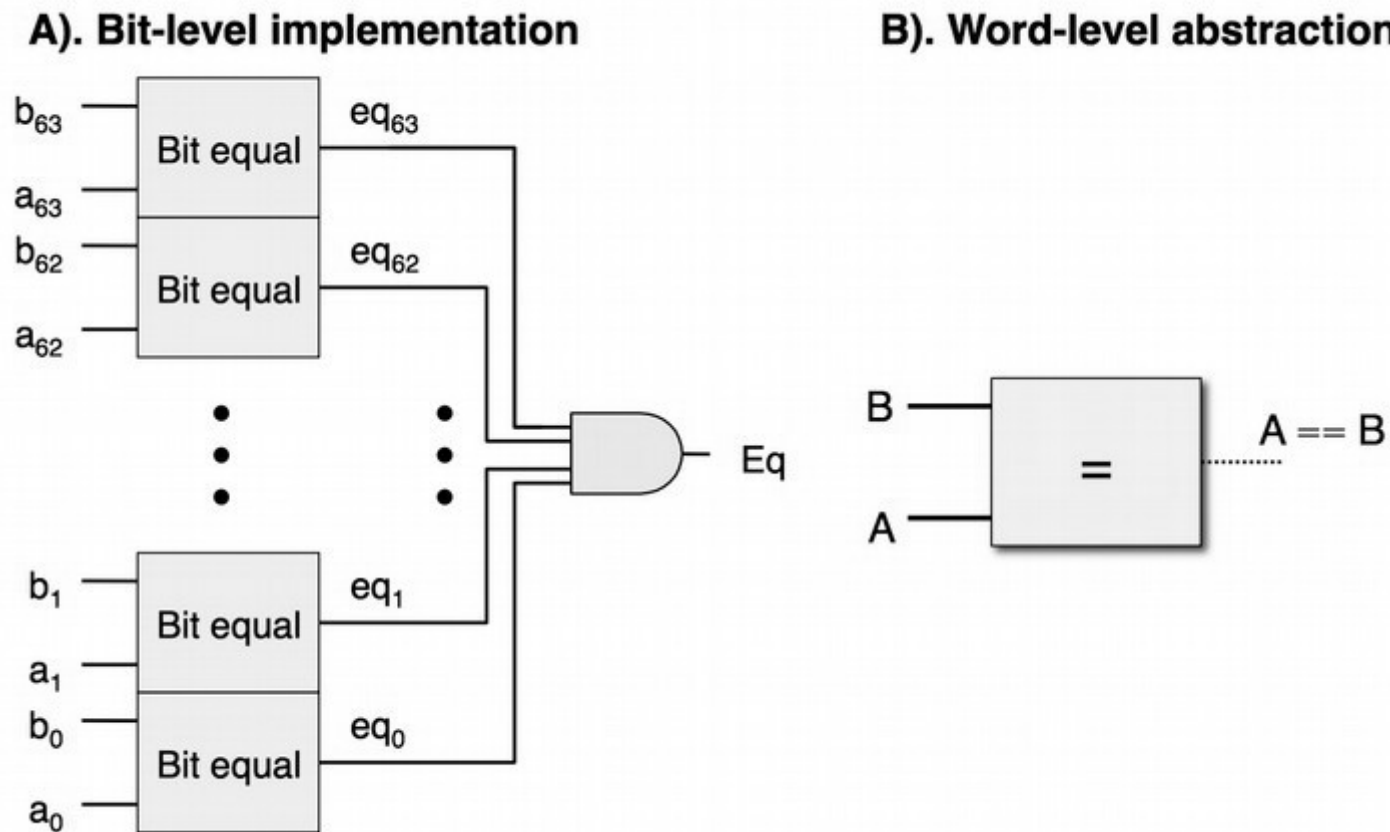
# Multiplexor (“selector”)



$$\text{MUX}(a, b, s) = (s \ \& \ a) \ | \ (!s \ \& \ b)$$

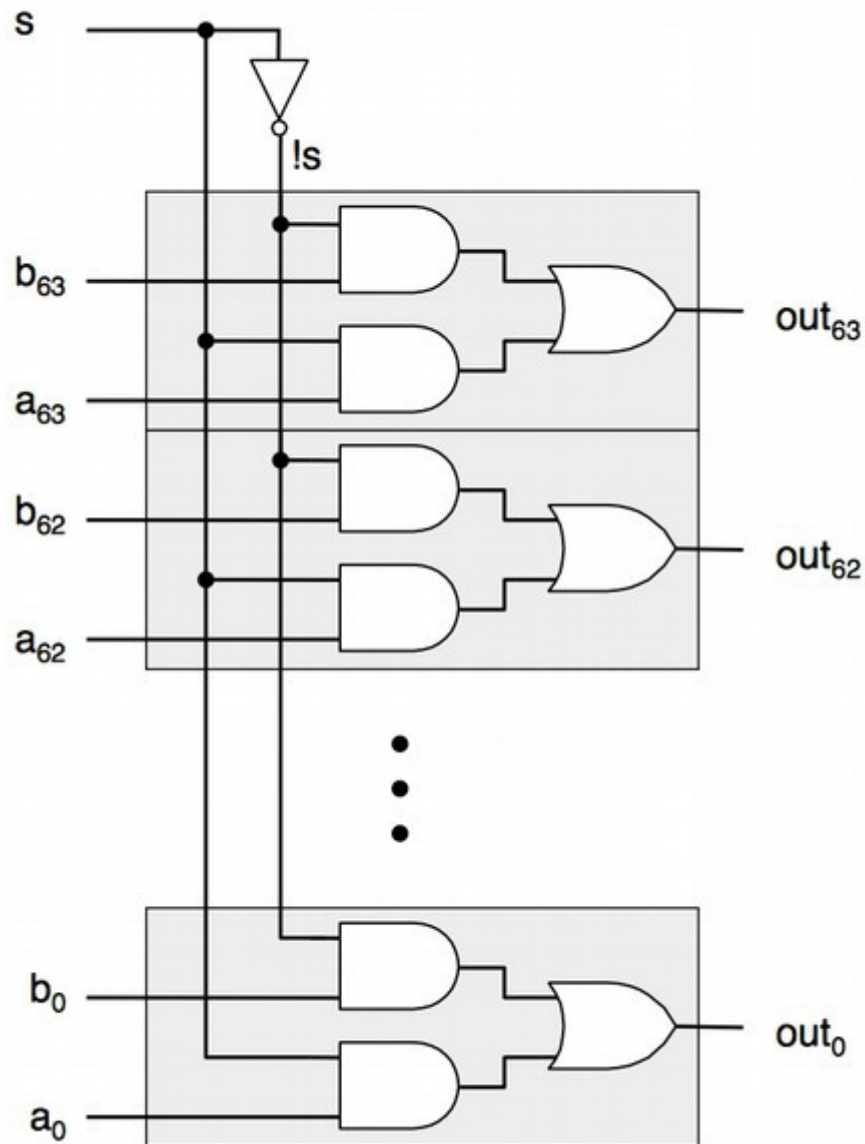
# Abstraction

- Name circuits, then use them to build more complex circuits
  - E.g., use bit-level EQ to build a word-level equality circuit:

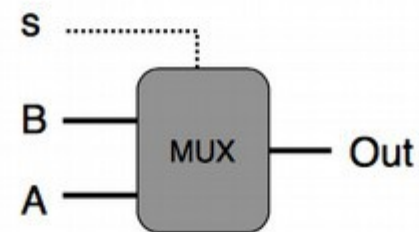


# Word-level 2-way multiplexer

A). Bit-level implementation



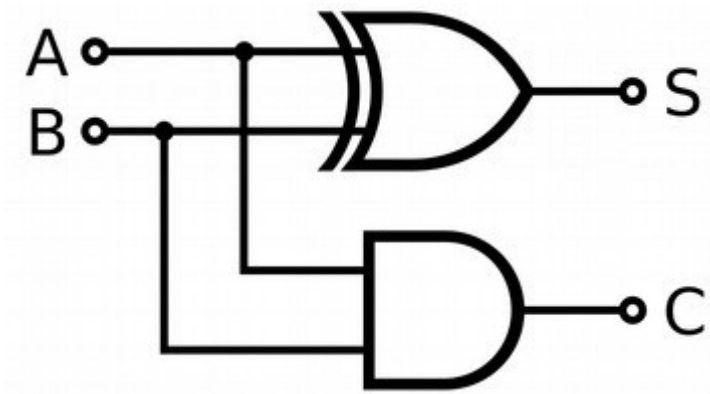
B). Word-level abstraction



```
int Out = [  
    s : A;  
    1 : B;  
];
```



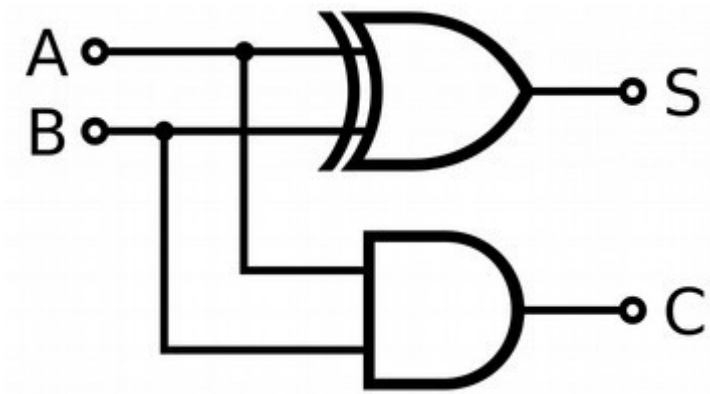
# Half adders



Half Adder

A	B	S	C
0	0	?	?
0	1	?	?
1	0	?	?
1	1	?	?

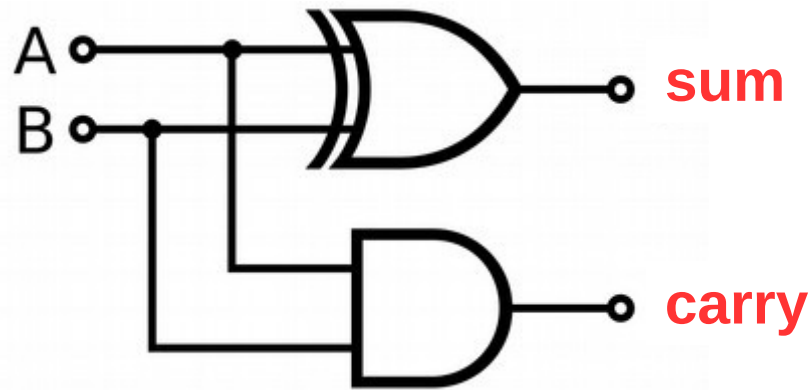
# Half adders



Half Adder

A	B	S	C
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

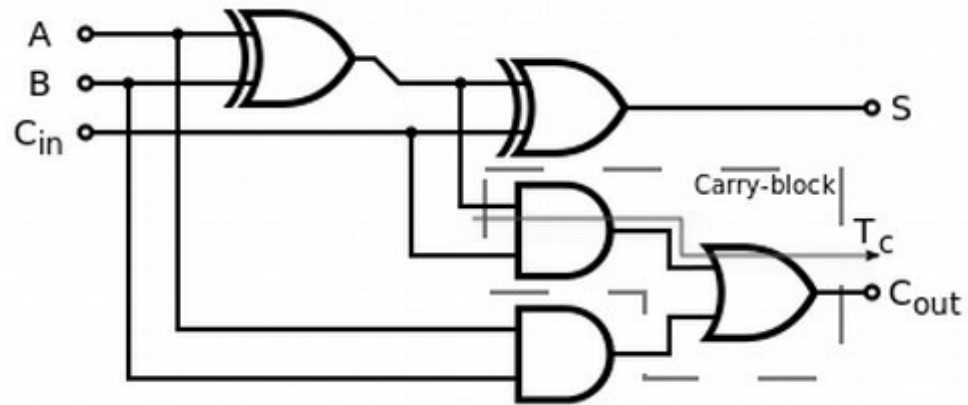
# Half adders



Half Adder

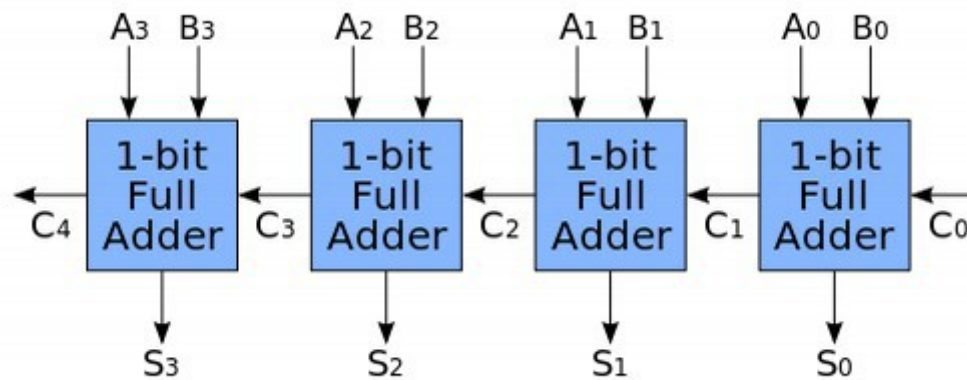
A	B	S	C
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

# Full adders

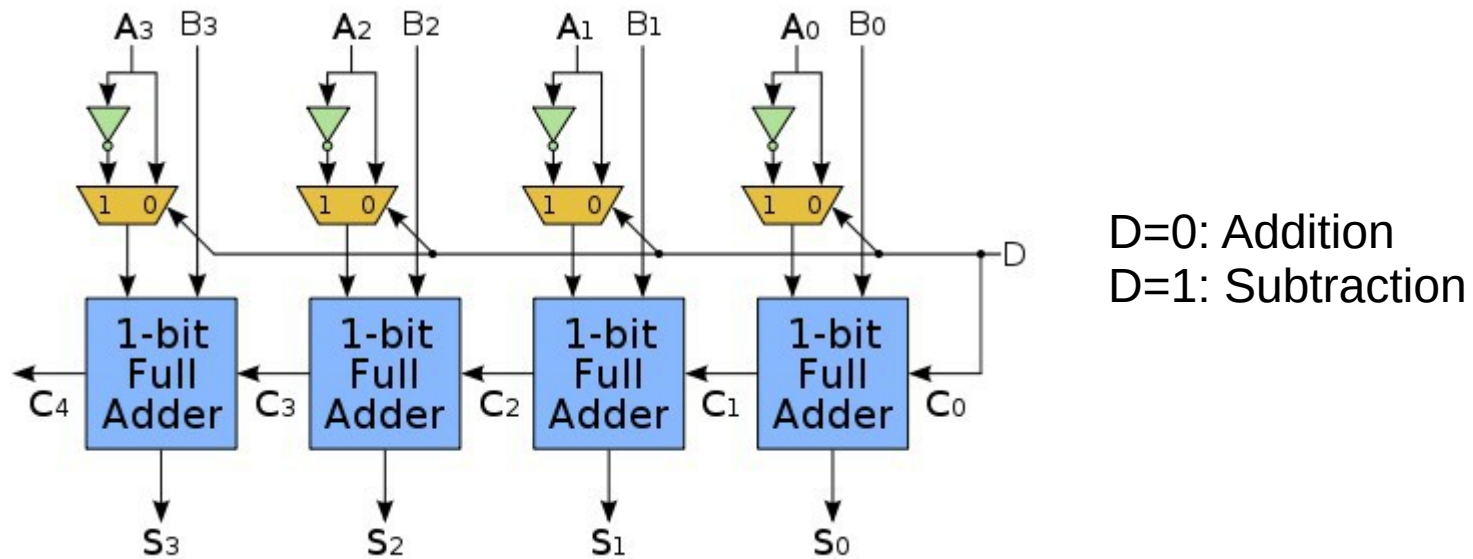


Full Adder

Connect full adders to build a **ripple-carry adder** that can handle multi-bit addition:



# Adder/subtractor



In two's complement:  $B - A = B + !A + 1$