## Learning Objectives

After completing this unit, you should be able to:

- Evaluate digital circuits that use AND, OR, XOR, and NOT.
- Convert binary integers to/from decimal, hexadecimal, ASCII.
- Identify the highest integer that can be represented with $n$ bits.
- Add 8-bit binary numbers without converting to/from decimal.
- Describe how RAM is organized (e.g., 8-bit cells, addresses).
- Describe how hard drives, optical drives, and flash drives work.


## Textbook Sections

1.1 Bits and Their Storage
1.2 Main Memory
1.3 Mass Storage
1.4 Representing Information as Bit Patterns
1.5 The Binary System

## Video Lectures

- Binary and Hex
- How Computer Memory Works
- How Hard Drives Work


## Assignments

Exercose02 Bits and Bytes; Chapter 1 Problems
Lab02 Binary Tutorial; Binary Cisco Challenges

## Exercise 2A: Bits and Bytes

Computer hardware is made up of billions of tiny electronic circuits that use low and high voltages to represent the values 0 and 1. These binary digits, or "bits" for short, are the building blocks of all digital technology.

## Model 1 Logic Gates

Complete the following tables based on the diagrams.


| AND |  |  |
| :--- | :---: | :---: |
| Inputs  Output  <br> 0 0   |  |  |
| 0 |  |  | 1



| XOR |  |
| :---: | :---: |
| Inputs | Output |
| 00 |  |
| 01 |  |
| 10 |  |
| 11 |  |


NOT

| Input | Output |  |  |
| :---: | :---: | :---: | :--- |
| 0 |  |  |  |
| 1 |  |  |  |

1. In the circuit diagrams, what does the color (brightness) of the the lines represent?
$\square$
2. For each type of gate, describe the circumstances when it will output the value 1 . AND:
$\square$

OR:
$\square$

XOR:
$\square$

NOT:
$\square$
3. What do you think a "logic gate" represents?
4. In the example circuit below, what are the values of $A, B, C, D$, and $E$ ?

5. How would $A, B, C, D$, and/or $E$ change if the top input were zero?

## Model 2 Binary Numbers

Assume there are four cards, one card with 8 dots, one card with 4 dots and one card with 2 dots and one card with 1 dot. Also assume the cards are ordered from left to right with the card with the most dots (8) to the card with the least dots (1). These are base 2 numbers, i.e., $2^{3}, 2^{2}$, $2^{1}$, and $2^{0}$. Below where the " 1 " appears means to use the card value and where the " 0 " appears to not use the value. The cards represent four binary digits, or in other words, a 4-bit number. What is the decimal number (base 10) each row represents?

6. In the table above, write the decimal value for each row by counting the number of dots.
a) What is the largest decimal number that can be represented by four bits?
$\square$
b) What is the smallest decimal number that can be represented by four bits?
$\square$
c) How many possible decimal numbers can be represented by four bits?
7. Examine the binary notation below the cards. Explain in a full sentence what a 0 means about the card's dots and what a 1 means.
$\square$
8. Complete the following table by writing the binary representation of the decimal numbers 0 to 15 using four bits. (And check your answers for \#6.)

| Decimal | Binary |  | Hex |  |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  |  |  | 0 |
| 1 |  |  |  | 1 |
| 2 |  |  |  | 2 |
| 3 |  |  |  | 3 |
| 4 |  |  |  | 4 |
| 5 |  |  |  | 5 |
| 6 |  |  |  | 6 |
| 7 |  |  |  | 7 |
| 8 |  |  |  | 8 |
| 9 |  |  |  | 9 |
| 10 |  |  |  | A |
| 11 |  |  |  | B |
| 12 |  |  |  | C |
| 13 |  |  |  | D |
| 14 |  |  |  | E |
| 15 |  |  |  | F |

9. Hexadecimal is shorthand for binary. For example, $0 x \mathrm{D} 5$ in hex is 11010101.
a) What is $0 \times 2 \mathrm{E}$ in binary? $\square$
b) What is $0 \times 74$ in binary? $\qquad$
c) What is $0 \times B 00$ in binary? $\square$
d) What is $0 x F A D$ in binary? $\qquad$
10. Based on the table in \#8, explain why binary is sometimes referred to as base-2, decimal as base-10, and hexadecimal as base-16.
11. Explain the humor: "There are only 10 types of people in the world: those who understand binary, and those who don't."
$\square$
12. Typically computers group 8 bits together at a time ( 8 bits are also called 1 byte). Fill in the number of dots for the four new cards:

13. What is the largest number that can be represented by:
a) five bits? $\qquad$ d) eight bits? $\square$
b) six bits? $\qquad$
e) $n$ bits? $\square$
c) seven bits? $\qquad$
14. Most computers built since the year 2000 have 64 -bit processors. Before then, 32 -bit processors were the norm. What is the advantage of having more bits?
$\square$
15. In terms of logic gates and digital circuits, what is the disadvantage of having more bits?
