

CS445 Linear Algebra Exercises

NAME:

With help from:

For this activity, your goal is to complete the exercises below, *and* to develop a Python-based answer key using numpy. After you complete each exercise by hand, update your Python script to print the key for that question.

Warning: There are two confusingly similar classes provided by numpy that can be used to represent matrices: `matrix` and `ndarray`. You may be tempted to use the `matrix` class to represent a matrix. Don't! It is deprecated and can only cause confusion.

1. Assuming that $B = \begin{bmatrix} 1 & 2 & -3 \\ 3 & 4 & -1 \end{bmatrix}$, $A = \begin{bmatrix} 2 & -5 & 1 \\ 1 & 4 & 5 \\ 2 & -1 & 6 \end{bmatrix}$, $y = \begin{bmatrix} 2 \\ -4 \\ 1 \end{bmatrix}$, $z = \begin{bmatrix} -15 \\ -8 \\ -22 \end{bmatrix}$

calculate each of the following:

(a) BA

(b) AB^T

(c) Ay

(d) $y^T z$ (This is the inner product, or dot product, of y and z .)

(e) yz^T (This is the outer product of y and z .)

2. Given that $A = \begin{bmatrix} 1 & 2 \\ 3 & 0 \end{bmatrix}$, and $b = \begin{bmatrix} 4 \\ 6 \end{bmatrix}$

(a) Find A^{-1} .

Check your answer by computing AA^{-1} .

(Hint: let $B = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ and solve $AB = I$ for a, b, c and d by solving a set of four equations in four unknowns. You would learn better ways to accomplish this in a linear algebra course, but this approach only requires high-school algebra.)

(b) Use A^{-1} to solve $Ax = b$ for x .

Check your answer by computing Ax .

3. (No need to include solutions to this question in your Python code.) Given the following matrices:

$$A = \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}, B = \begin{bmatrix} -2 & 0 \\ 0 & 2 \end{bmatrix}, C = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}, D = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$

Draw and label each of the following:

Ax , Bx , Cx , Dx

